- Rating Estimation in MD Recomender Systems

Combined Reduction-Based and Traditional CF Approaches

### **Outline**

# Rating Estimation in MD Recomender Systems Combined Reduction-Based and Traditional CF Approaches

Multi-Level Rating Estimation Problem

Implementation and Evaluation of MD Approach
Experimental Setup
Evaluating the Reduction-Based Approach

# Performance Metric

#### Will help to determine which method performs better

- MAE is an example of statistical accuracy measure
- F-measure is an example of decision-support accuracy metric
- The latter suit recommender systems better

### $\mu_{A,X}(Y)$ is an abstract performance metric where

- ► A a recommendation algorithm
- X training set of known ratings
- ▶ Y evaluation set of known ratings , where  $X \cup Y = \emptyset$

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# Performance Metric II

For each  $d \in Y$ 

- d.R is user-specified rating for that data point
- ▶ d.R<sub>A,X</sub> is rating predicted by algorithm A trained on X

Then  $\mu_{A,X}(Y)$  for MAE is defined as

$$\mu_{A,X}(Y) = \frac{1}{|Y|} \sum_{d \in Y} |d.R_{A,X} - d.R|$$

We assume that A is a traditional collaborative filtering method

# **Combined Approach**

- Use known ratings to determine contextual segments that outperform traditional CF method (offline)
- Predict the rating by using the best contextual segment and the 2D recommendation algorithm (real-time)

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# **Determining High-Performing Contextual Segments**

Input:  $T, R_{A,T}, \mu, N$ 

**Ouput:** SEGM(T) - a set of contextual segments on which the reduction-based approach on algorithm A outperforms the pure algorithm A.

### Algorithm:

- Let SEGM(T) initially be the set of all large contextual segments for the set or ratings T.
- 2. For each segment  $S \in SEGM(T)$  compute  $\mu_{A,S}(S)$  and  $\mu_{A,T}(S)$ . Keep only those for which  $\mu_{A,S}(S) \gg \mu_{A,T}(S)$
- 3. Discard  $S \in SEGM(T)$  for which  $\exists Q : S \subset Q, \mu_{A,Q}(Q) > \mu_{A,S}(S)$

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# Estimating the Rating

**Input:**  $SEGM(T) = \{S_1, \dots, S_k\}$  where  $\mu_{A,S_i}(S_i) \ge \mu_{A,S_i}(S_j), i \ge j$ 

d – data point for which we want to estimate the rating

**Output:** d.R – estimated rating for d.

Algorithm:

A picture from paper goes here

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# Multi-Level Rating Estimation Problem

Estimate unknown individual ratings in terms of known aggregate and known individual ratings.

- ► *R*(*JD*, *action*) = 6
- ightharpoonup R(JD, Gladiator) = 7
- ► *R*(*JD*, *Matrix*) = 3
- $\Rightarrow R(JD, OtherMovie) = ?$

# More Formal Definition

#### Assume

- $ightharpoonup R_a(JD, action)$  actual rating assigned by JD himself
- $ightharpoonup R_c(JD, action)$  rating computed from individual ratings R(JD, x)
- $\triangleright$   $X_r$  a set of action movies that John has already rated
- ▶  $X_{nr}$  a set of yet unrated action movies,  $X_r \cup X_{nr} = action$

Assign ratings to 
$$R(JD,x), x \in X_{nr}$$
 to minimize  $|R_a(JD,action) - R_c(JD,action)|$ 

▶ There might be infinite number of solutions

Multi-Level Rating Estimation Problem

# Linear Example

#### Assume

- AVG is the aggregation function
- $X_{nr} = \{y_1, \dots, y_k\}$

Then we want to find  $R(JD, y_1), \dots, R(JD, y_k)$  s.t.

- $ightharpoonup R(JD, y_1) + \ldots + R(JD, y_k) = c$
- $c = (|X_r| + |X_{nr}|) \cdot R_a(JD, action) \sum_{x \in X_r} R(JD, x)$

# Another Reason for Aggregate Hierarchies

### Under some assumptions

► The estimation error for aggregate rating is smaller than the estimation error for individual ratings.

#### The assumptions are

- the rating estimation function  $R_c(u,i) = R_a(u,i) + \varepsilon(\mu,\sigma^2)$
- the rating aggregation function (AVG)
- the accuracy measure (MAE)

The general case is an open research question.

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# Setup for Evaluation

- Implement a movie RS
- Unlike MovieLens add contextual information
  - When, Where, With whom
- No aggregation hierarchies
  - Show that contextual information does matter
  - Reduction-based approach does not fit with aggregation hierarchies
  - Use of hierarchies requires larger amounts of more detailed data

# **Contextual Dimensions**

- ► Time (Weekday, weekend, don't remember)
  - If seen on weekend, was it opening weekend for the movie (yes, no, don't remember)
- Place (cinema, home, don't remember)
- Companion (alone, with friends, boyfriend/girlfriend, family, others)

<sup>-</sup> Implementation and Evaluation of MD Approach

Experimental Setup

Experimental Setup

# **Data Collection**

- Rate movies from 1 to 13
- Participants were 117 college students
- 1755 ratings entered over a period of 12 months
- Those who rated fewer than 10 movies were dropped out
- Finally 1457 ratings from 62 students for 202 movies
- ▶ 10% evaluation dataset (D<sub>E</sub>)
- ▶ 90% modelling dataset (D<sub>M</sub>)

# Significance of Dimensions

Which dimensions make significant difference in rating estimations?

- ▶ Partition ratings into categories, e.g. *Time* and *Place*
- Compute average rating per student in each category
- Apply a paired comparison test (t-test)

All dimensions appear to be significant.

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Incorporating Contextual Information in Recommender Systems Using a Multidimensional Approach

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Levaluating the Reduction-Based Approach