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# Neural Networks

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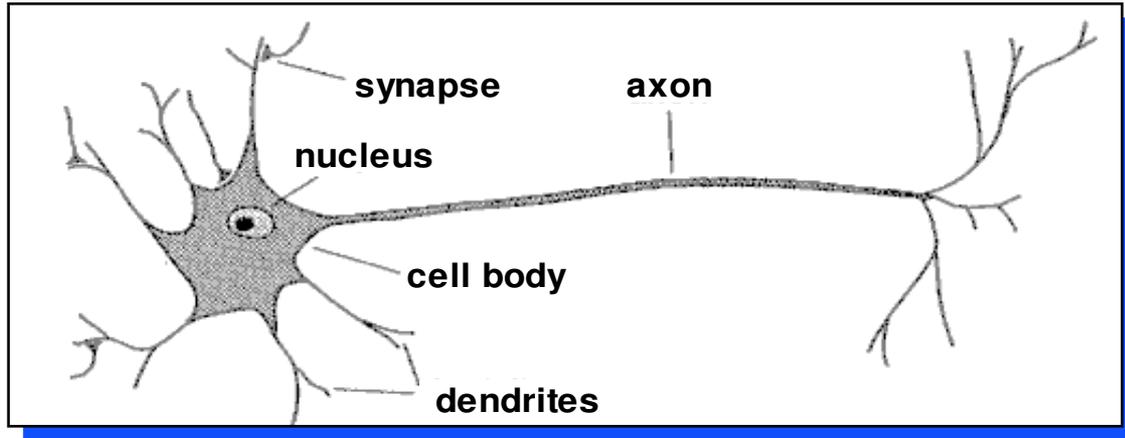
## Recently published articles

- Clonal Selection - An Immunological Algorithm for Global Optimization over Continuous Spaces
- Swarm Intelligence Heuristics for Graph Coloring Problem
- O-BEE-COL: Optimal BEES for COLoring Graphs
- Escaping Local Optima via Parallelization and Migration Protein Multiple Sequence Alignment by Hybrid Bio-Inspired Algorithms
- Effective Calibration of Artificial Gene Regulatory Networks
- Large scale agent-based modeling of the humoral and cellular immune response
- A Memetic Immunological Algorithm for Resource Allocation Problem.

# Biological inspirations

- Some numbers...
  - The human brain contains about 10 billion nerve cells (neurons)
  - Each neuron is connected to the others through 10000 synapses
- Properties of the brain
  - It can learn, reorganize itself from experience
  - It adapts to the environment
  - It is robust and fault tolerant

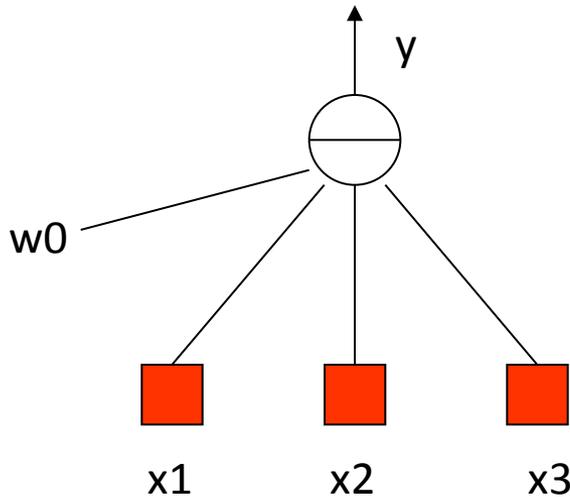
# Biological neuron



- A neuron has
  - A branching input (dendrites)
  - A branching output (the axon)
- The information circulates from the dendrites to the axon via the cell body
- Axon connects to dendrites via synapses
  - Synapses vary in strength
  - Synapses may be excitatory or inhibitory

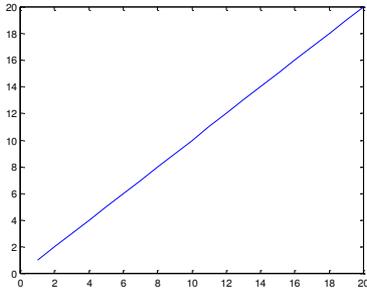
# What is an artificial neuron ?

- Definition : Non linear, parameterized function with restricted output range



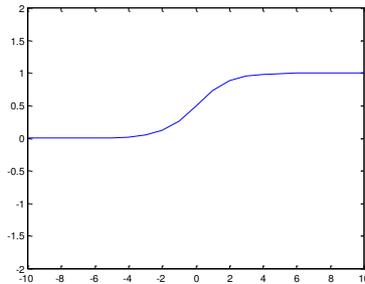
$$y = f \left( w_0 + \sum_{i=1}^{n-1} w_i x_i \right)$$

# Activation functions



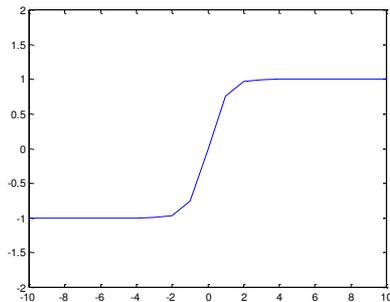
Linear

$$y = x$$



Logistic

$$y = \frac{1}{1 + \exp(-x)}$$



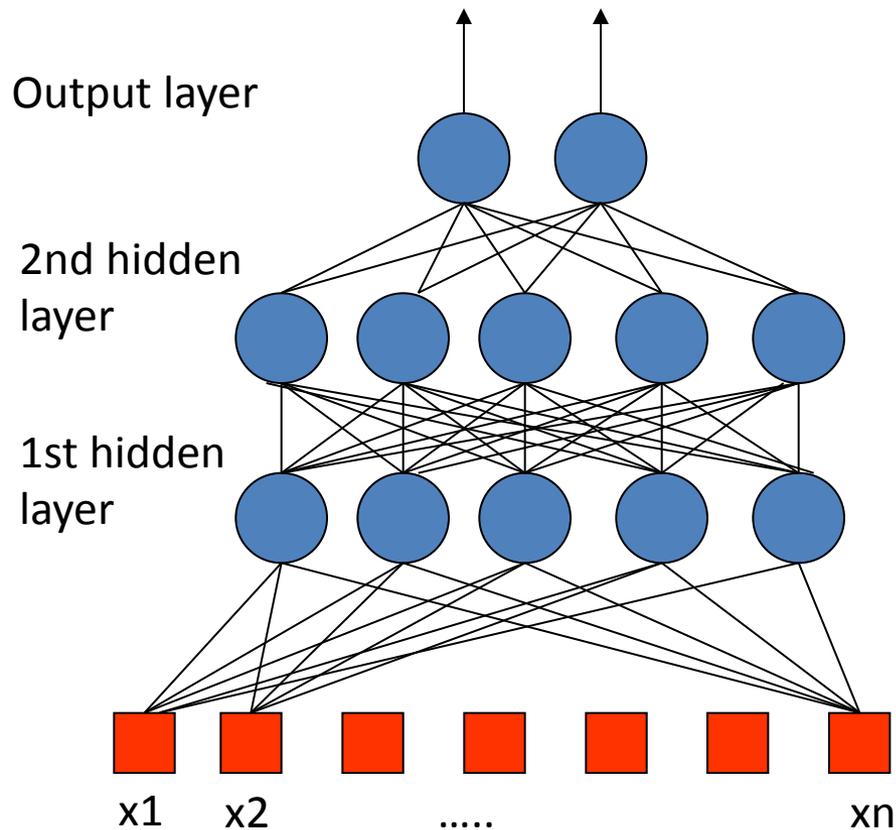
Hyperbolic tangent

$$y = \frac{\exp(x) - \exp(-x)}{\exp(x) + \exp(-x)}$$

# Neural Networks

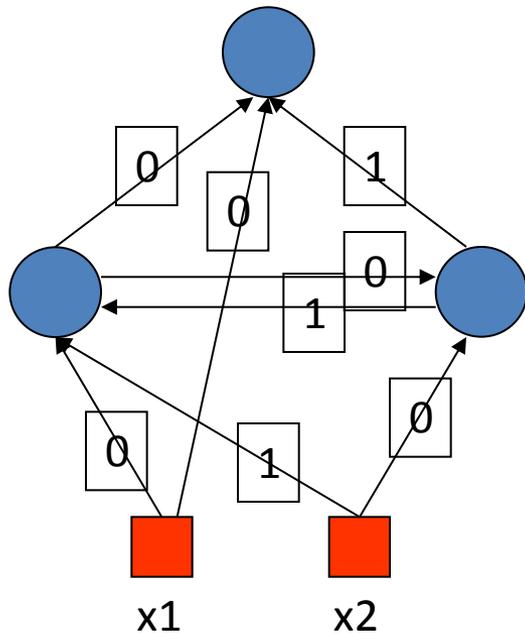
- A mathematical model to solve engineering problems
  - Group of highly connected neurons to realize compositions of non linear functions
- Tasks
  - Classification
  - Discrimination
  - Estimation
- 2 types of networks
  - Feed forward Neural Networks
  - Recurrent Neural Networks

# Feed Forward Neural Networks



- The information is propagated from the inputs to the outputs
- Computations of **No** non linear functions from **n** input variables by compositions of **Nc** algebraic functions
- Time has no role (NO cycle between outputs and inputs)

# Recurrent Neural Networks



- Can have arbitrary topologies
- Can model systems with internal states (dynamic ones)
- Delays are associated to a specific weight
- Training is more difficult
- Performance may be problematic
  - Stable Outputs may be more difficult to evaluate
  - Unexpected behavior (oscillation, chaos, ...)

# Learning

- The procedure that consists in estimating the parameters of neurons so that the whole network can perform a specific task
- 2 types of learning
  - The supervised learning
  - The unsupervised learning
- The Learning process (supervised)
  - Present the network a number of inputs and their corresponding outputs
  - See how closely the actual outputs match the desired ones
  - Modify the parameters to better approximate the desired outputs

# Supervised learning

- The desired response of the neural network in function of particular inputs is well known.
- A “Professor” may provide examples and teach the neural network how to fulfill a certain task

# Unsupervised learning

- Idea : group typical input data in function of resemblance criteria un-known a priori
- Data clustering
- No need of a professor
  - The network finds itself the correlations between the data
  - Examples of such networks :
    - Kohonen feature maps

# Properties of Neural Networks

- Supervised networks are universal approximators (Non recurrent networks)
- **Theorem : Any limited function can be approximated by a neural network with a finite number of hidden neurons to an arbitrary precision**
- Type of Approximators
  - Linear approximators : for a given precision, the number of parameters grows exponentially with the number of variables (polynomials)
  - Non-linear approximators (NN), the number of parameters grows linearly with the number of variables

# Other properties

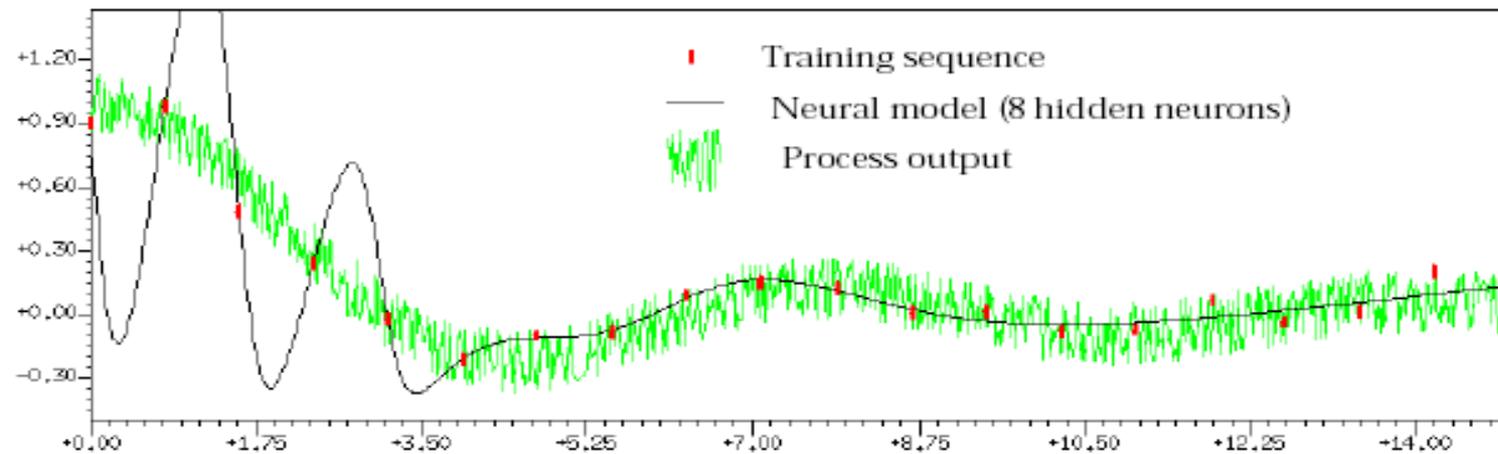
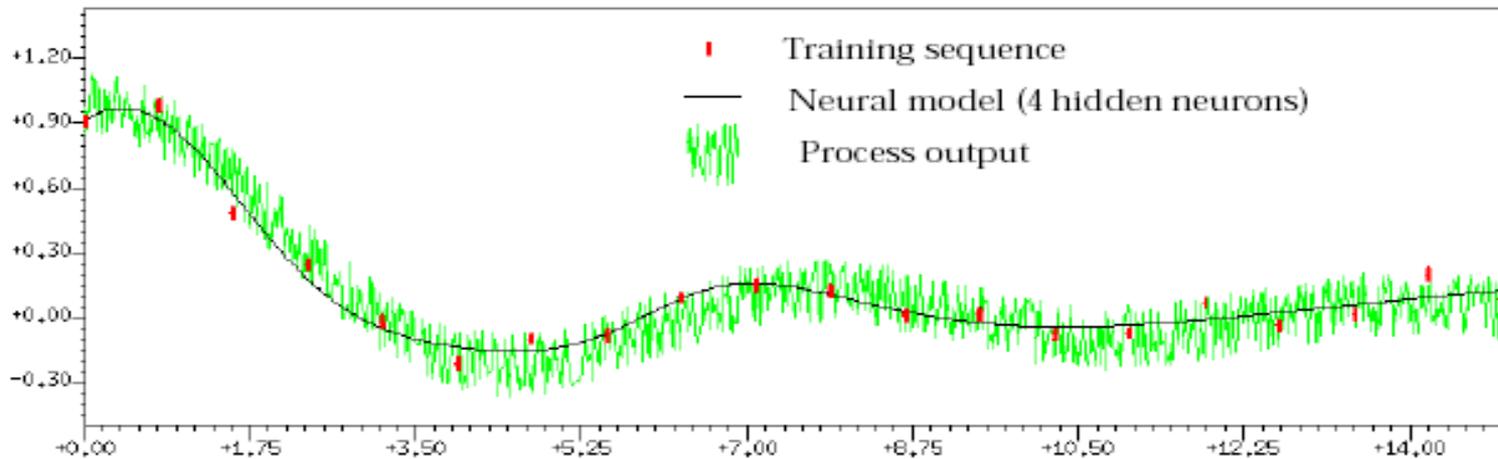
- **Adaptivity**
  - Adapt weights to environment and retrained easily
- **Generalization ability**
  - May provide against lack of data
- **Fault tolerance**
  - Graceful degradation of performances if damaged => The information is distributed within the entire net.

# Static modeling

- In practice, it is rare to approximate a known function by a uniform function
- “black box” modeling : model of a process
- The  $y$  output variable depends on the input variable  $x$  with  $k=1$  to  $N$   $\{x^k, y_p^k\}$
- Goal : Express this dependency by a function, for example a neural network

- If the learning ensemble results from measures, the noise intervenes
- Not an approximation but a fitting problem
- Regression function
- Approximation of the regression function : Estimate the more probable value of  $y_p$  for a given input  $x$
- Cost function:
$$J(w) = \frac{1}{2} \sum_{k=1}^N [y_p(x^k) - g(x^k, w)]^2$$
- Goal: Minimize the cost function by determining the right function  $g$

# Example



# Classification (Discrimination)

- Class objects in defined categories
- Rough decision OR
- Estimation of the probability for a certain object to belong to a specific class

Example : Data mining

- Applications : Economy, speech and patterns recognition, sociology, etc.

# Example

65473      60198      68544  
70065    70117    19032<sup>ZIP</sup>    96720  
27260      61820      19559  
74136      ~~19137~~      63101  
20878      60521      38002  
48640-2398    20907      14868

Examples of handwritten postal codes  
drawn from a database available from the US Postal service

# What do we need to use NN ?

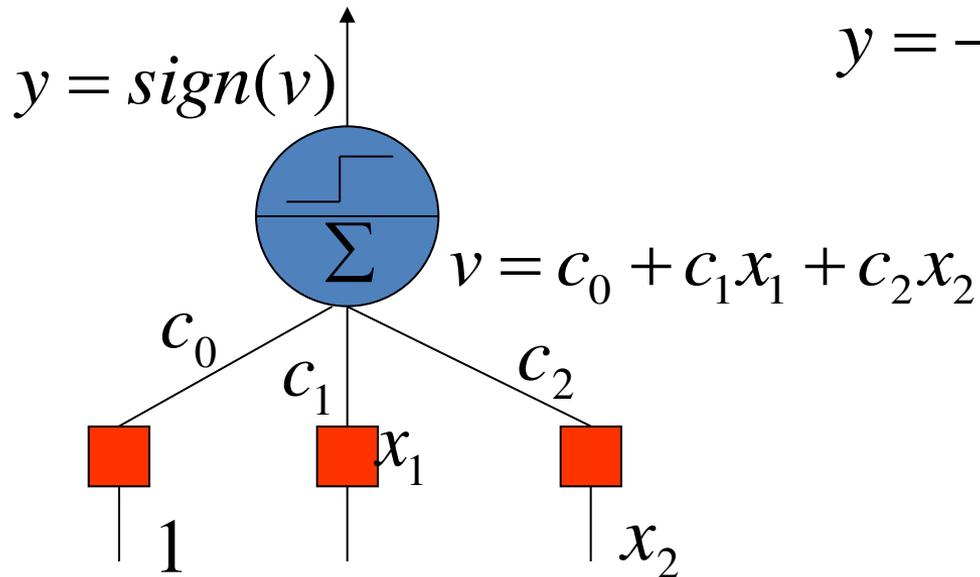
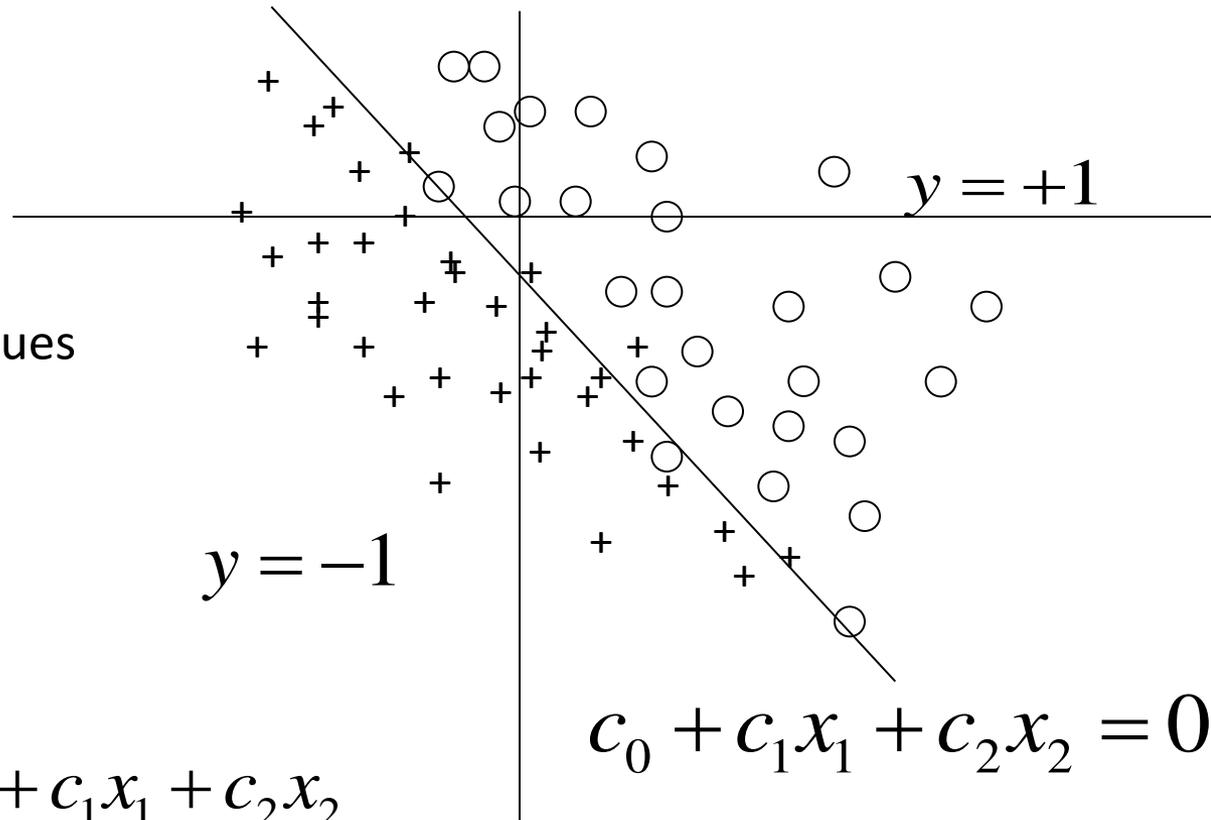
- Determination of pertinent inputs
- Collection of data for the learning and testing phase of the neural network
- Finding the optimum number of hidden nodes
- Estimate the parameters (Learning)
- Evaluate the performances of the network
- IF performances are not satisfactory then review all the precedent points

# Classical neural architectures

- Perceptron
- Multi-Layer Perceptron
- Radial Basis Function (RBF)
- Kohonen Features maps
- Other architectures
  - An example : Shared weights neural networks

# Perceptron

- Rosenblatt (1962)
- Linear separation
- Inputs : Vector of real values
- Outputs : 1 or -1



# Learning (The perceptron rule)

- Minimization of the cost function :  $J(c) = \sum_{k \in M} -y_p^k v^k$

- $J(c)$  is always  $\geq 0$  ( $M$  is the ensemble of bad classified examples)

- $y_p^k$  is the target value

- Partial cost

– If  $x^k$  is not well classified :  $J^k(c) = -y_p^k v^k$

– If  $x^k$  is well classified  $J^k(c) = 0$

- Partial cost gradient



$$\frac{\partial J^k(c)}{\partial c} = -y_p^k x^k$$

- Perceptron algorithm

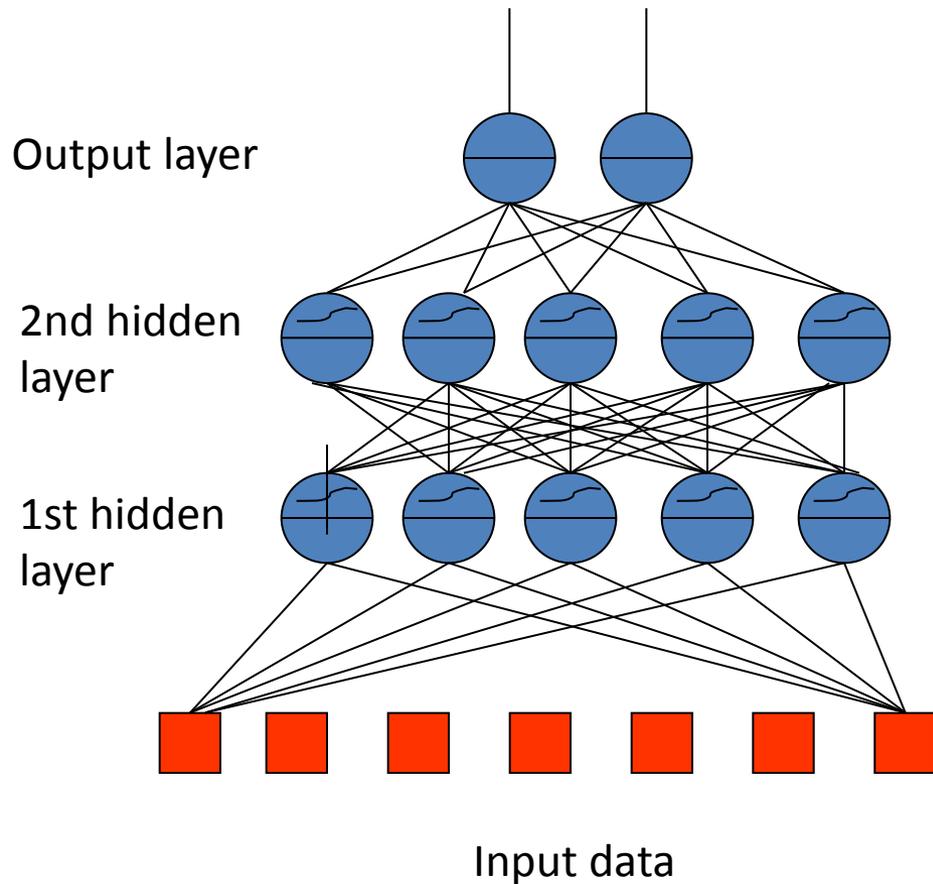
if  $y_p^k v^k > 0$  ( $x^k$  is well classified) :  $c(k) = c(k-1)$

if  $y_p^k v^k < 0$  ( $x^k$  is not well classified) :  $c(k) = c(k-1) + y_p^k x^k$

- The perceptron algorithm converges if examples are linearly separable

# Multi-Layer Perceptron

- One or more hidden layers
- Sigmoid activation functions



# Learning

- Back-propagation algorithm

$$net_j = w_{j0} + \sum_i^n w_{ji} o_i$$

$$o_j = f_j(net_j)$$

$$\Delta w_{ji} = -\alpha \frac{\partial E}{\partial w_{ji}} = -\alpha \frac{\partial E}{\partial net_j} \frac{\partial net_j}{\partial w_{ji}} = \alpha \delta_j o_i$$

Credit assignment

$$\delta_j = -\frac{\partial E}{\partial net_j}$$


$$\delta_j = -\frac{\partial E}{\partial o_j} \frac{\partial o_j}{\partial net_j} = -\frac{\partial E}{\partial o_j} f'(net_j)$$

$$E = \frac{1}{2} (t_j - o_j)^2 \Rightarrow \frac{\partial E}{\partial o_j} = -(t_j - o_j)$$

$$\delta_j = (t_j - o_j) f'(net_j)$$

If the jth node is an output unit

$$\frac{\partial E}{\partial o_j} = \sum_k^{\kappa} \frac{\partial E}{\partial net_k} \frac{\partial net_k}{\partial o_j} = - \sum_k^{\kappa} \delta_k w_{kj}$$

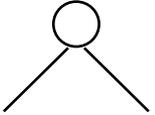
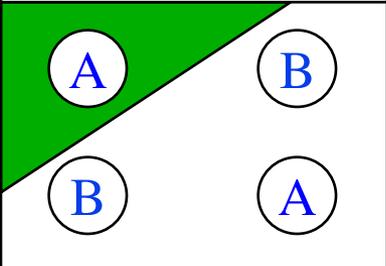
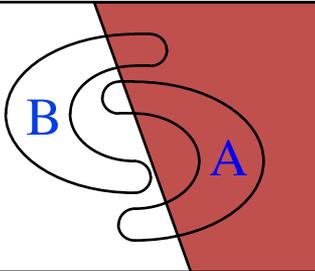
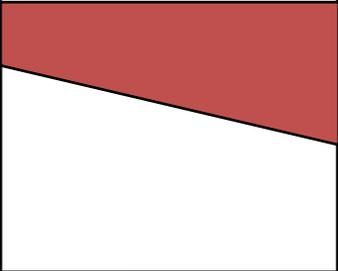
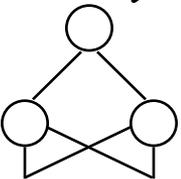
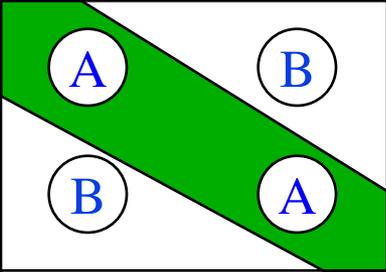
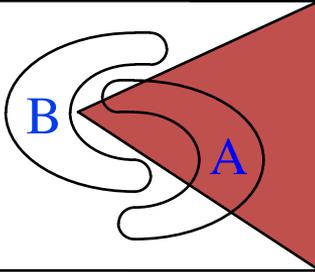
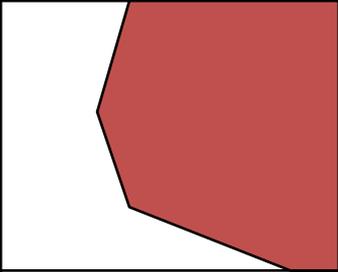
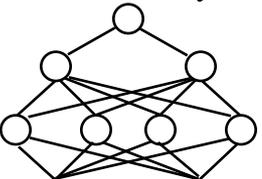
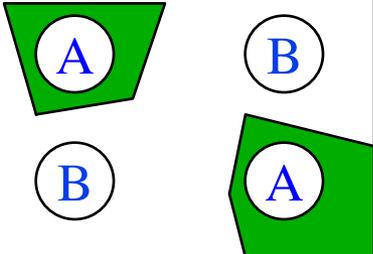
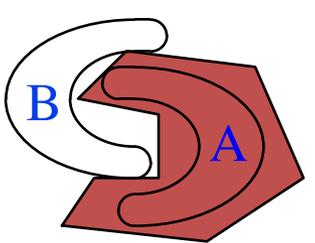
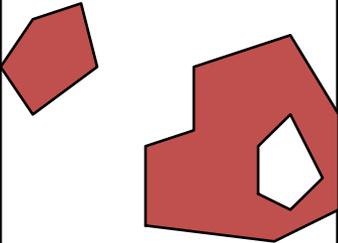
$$\delta_j = f'_j(net_j) \sum_k^{\kappa} \delta_k w_{kj}$$

$$\Delta w_{ji}(t) = \alpha \delta_j(t) o_i(t) + \gamma \Delta w_{ji}(t-1)$$

Momentum term to smooth  
The weight changes over time

$$w_{ji}(t) = w_{ji}(t-1) + \Delta w_{ji}(t)$$

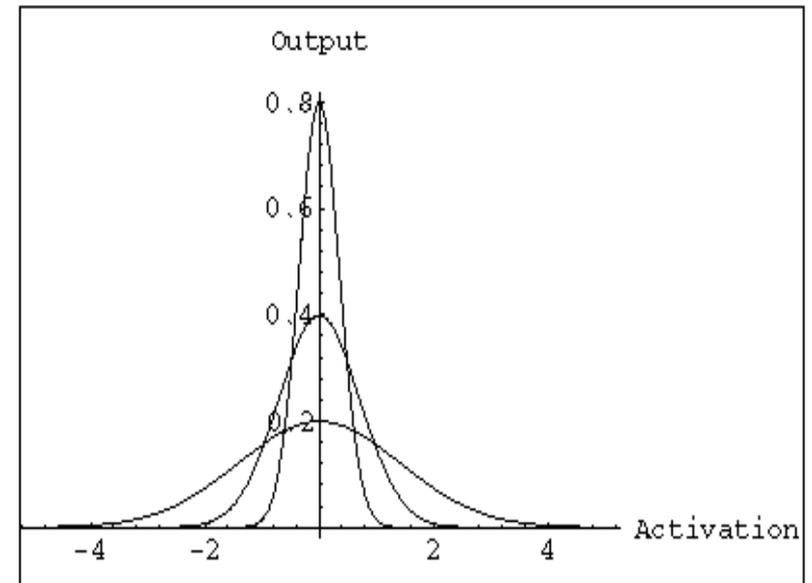
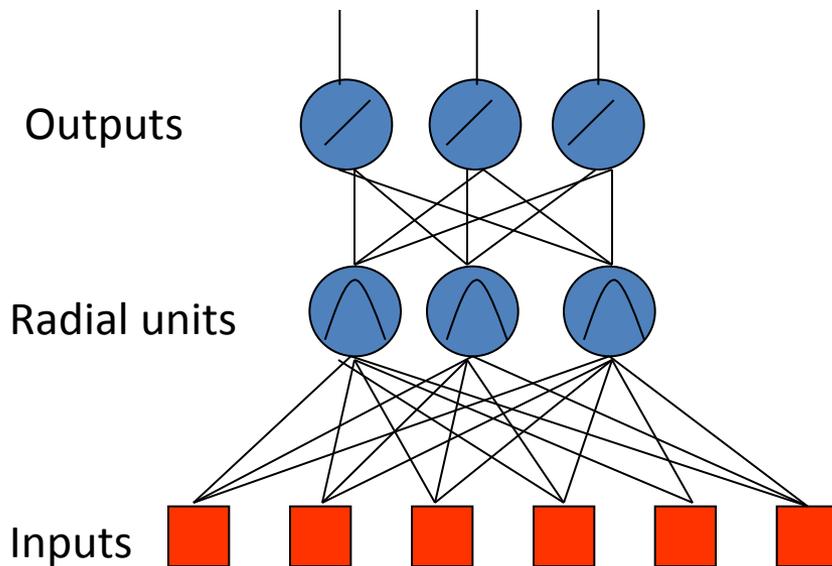
# Different non linearly separable problems

| <i>Structure</i>   | <i>Types of Decision Regions</i>                             | <i>Exclusive-OR Problem</i>  | <i>Classes with Meshed regions</i>  | <i>Most General Region Shapes</i>   |
|--|--|--|---|---|
| <p><i>Single-Layer</i></p>  | <p><i>Half Plane Bounded By Hyperplane</i></p>               |    |    |    |
| <p><i>Two-Layer</i></p>    | <p><i>Convex Open Or Closed Regions</i></p>                  |   |   |   |
| <p><i>Three-Layer</i></p>  | <p><i>Arbitrary (Complexity Limited by No. of Nodes)</i></p> |  |  |  |

# Radial Basis Functions (RBFs)

- Features

- One hidden layer
- The activation of a hidden unit is determined by the distance between the input vector and a prototype vector



- RBF hidden layer units have a receptive field which has a centre
- Generally, the hidden unit function is Gaussian
- The output Layer is linear
- Realized function

$$s(x) = \sum_{j=1}^K W_j \Phi(\|x - c_j\|)$$

$$\Phi(\|x - c_j\|) = \exp\left(-\left(\frac{\|x - c_j\|}{\sigma_j}\right)^2\right)$$

# Learning

- The training is performed by deciding on
  - How many hidden nodes there should be
  - The centers and the sharpness of the Gaussians
- 2 steps
  - In the 1st stage, the input data set is used to determine the parameters of the basis functions
  - In the 2nd stage, functions are kept fixed while the second layer weights are estimated ( Simple BP algorithm like for MLPs)

# MLPs versus RBFs

- **Classification**

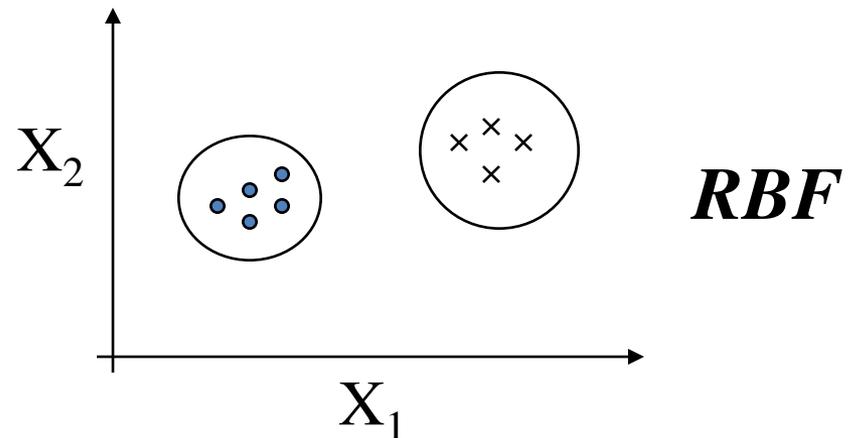
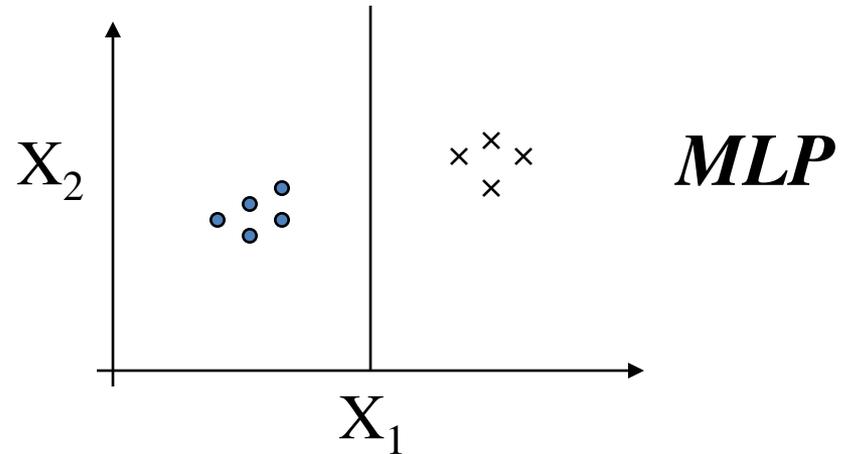
- MLPs separate classes via hyperplanes
- RBFs separate classes via hyperspheres

- **Learning**

- MLPs use distributed learning
- RBFs use localized learning
- RBFs train faster

- **Structure**

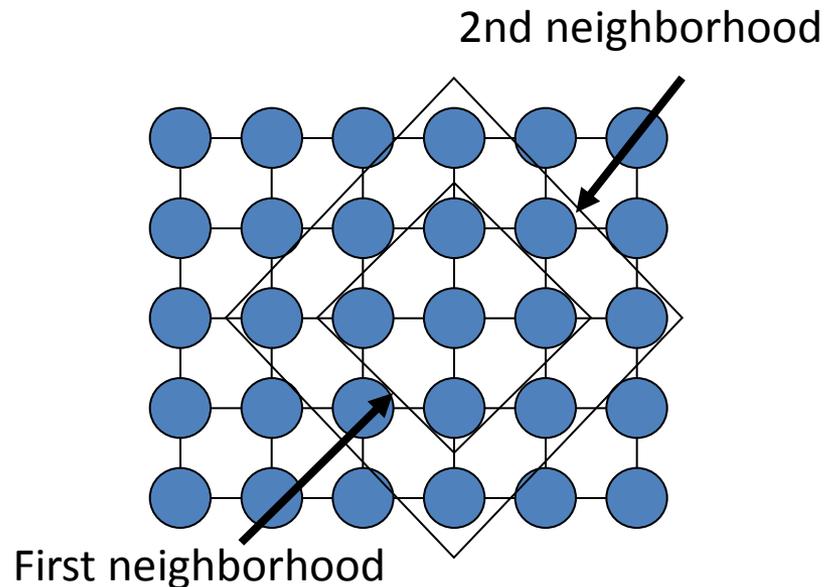
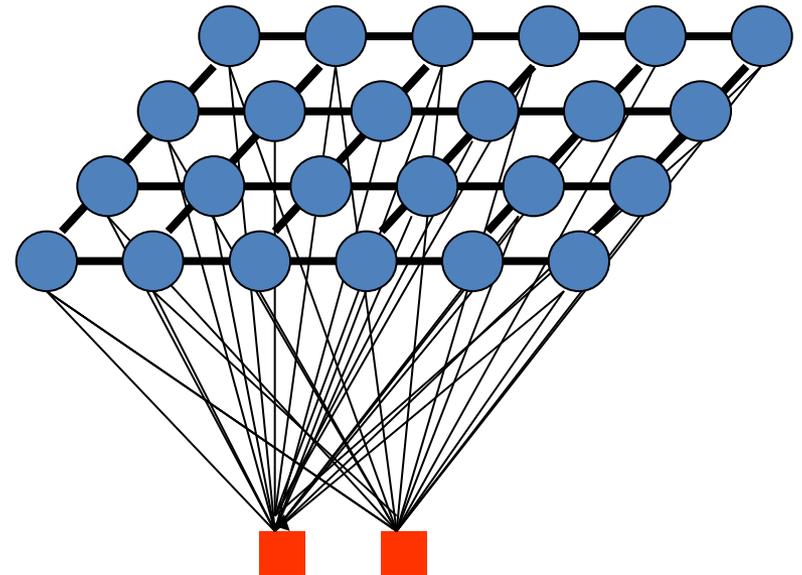
- MLPs have one or more hidden layers
- RBFs have only one layer
- RBFs require more hidden neurons => curse of dimensionality



# Self organizing maps

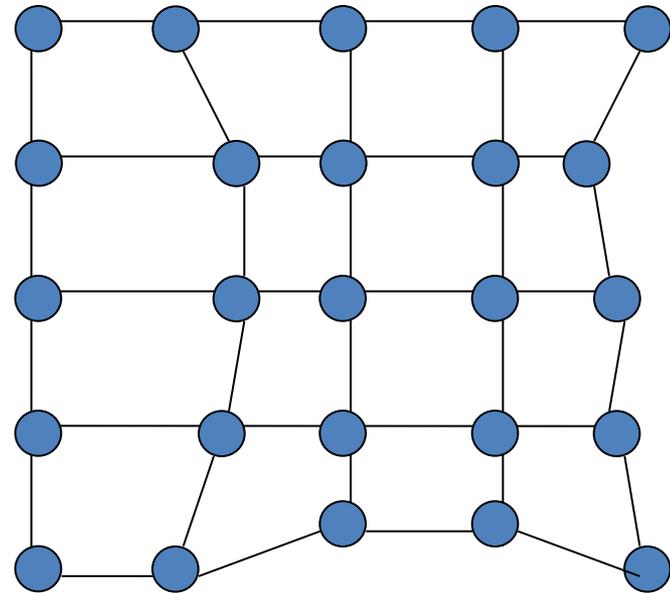
- The purpose of SOM is to map a multidimensional input space onto a topology preserving map of neurons
  - Preserve a topological so that neighboring neurons respond to « similar » input patterns
  - The topological structure is often a 2 or 3 dimensional space
- Each neuron is assigned a weight vector with the same dimensionality of the input space
- Input patterns are compared to each weight vector and the closest wins (Euclidean Distance)

- The activation of the neuron is spread in its direct neighborhood => neighbors become sensitive to the same input patterns
- Block distance
- The size of the neighborhood is initially large but reduce over time => Specialization of the network



# Adaptation

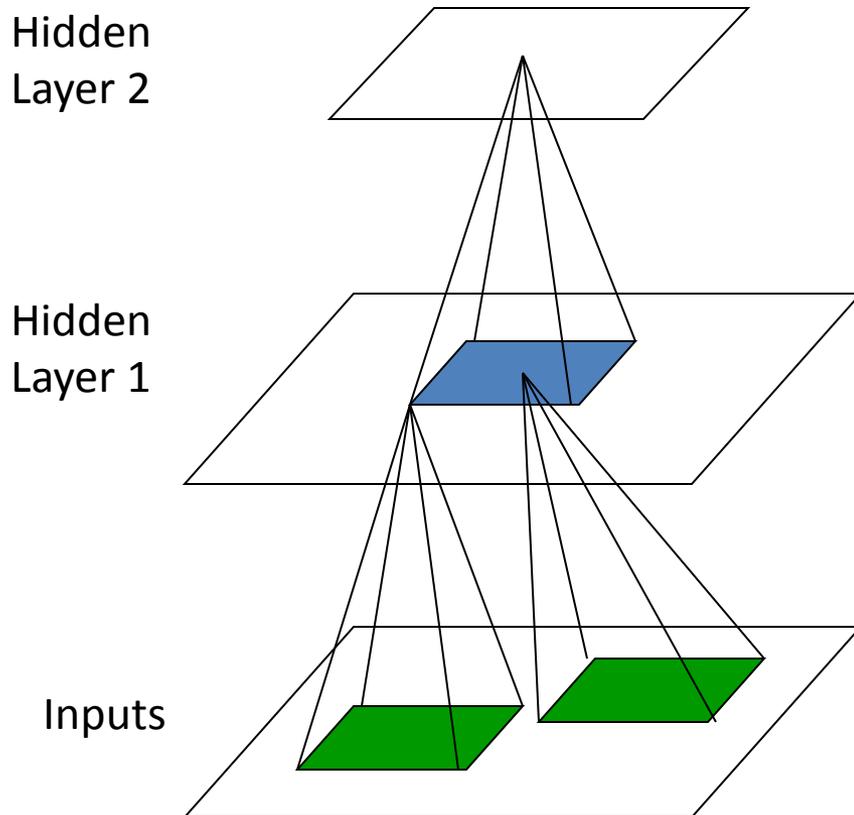
- During training, the “winner” neuron and its neighborhood adapts to make their weight vector more similar to the input pattern that caused the activation
- The neurons are moved closer to the input pattern
- The magnitude of the adaptation is controlled via a learning parameter which decays over time



# Shared weights neural networks: Time Delay Neural Networks (TDNNs)

- Introduced by Waibel in 1989
- Properties
  - Local, shift invariant feature extraction
  - Notion of receptive fields combining local information into more abstract patterns at a higher level
  - Weight sharing concept (All neurons in a feature share the same weights)
    - All neurons detect the same feature but in different position
- Principal Applications
  - Speech recognition
  - Image analysis

# TDNNs (cont'd)



- Objects recognition in an image
- Each hidden unit receive inputs only from a small region of the input space : receptive field
- Shared weights for all receptive fields => translation invariance in the response of the network

- Advantages

- Reduced number of weights

- Require fewer examples in the training set

- Faster learning

- Invariance under time or space translation

- Faster execution of the net (in comparison of full connected MLP)

# Neural Networks (Applications)

- Face recognition
- Time series prediction
- Process identification
- Process control
- Optical character recognition
- Adaptative filtering
- Etc...

# Conclusion on Neural Networks

- Neural networks are utilized as statistical tools
  - Adjust non linear functions to fulfill a task
  - Need of multiple and representative examples but fewer than in other methods
- Neural networks enable to model complex static phenomena (FF) as well as dynamic ones (RNN)
- NN are good classifiers BUT
  - Good representations of data have to be formulated
  - Training vectors must be statistically representative of the entire input space
  - Unsupervised techniques can help
- The use of NN needs a good comprehension of the problem

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