# Modeling Agent-Based Traffic Simulation Properties in Alloy

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## Abstract

The advances in Intelligent Transportation Systems (ITS) call for a new generation of traffic simulation models that support connectivity and collaboration among simulated vehicles and traffic infrastructure. In this paper we introduce MATISSE, a complex, large scale agent-based framework for the modeling and simulation of ITS and discuss how Alloy, a modeling language based on set theory and first order logic, was used to specify, verify, and analyze MATISSE's traffic models.

## 1. INTRODUCTION

For the past twenty years, Intelligent Transportation Systems (ITS) have been considered as possible solutions for the traffic safety and congestion problems. ITS are defined as "the application of advanced sensor, computer, electronics, and communication technologies and management strategies in an integrated manner to increase the safety and efficiency of the surface transportation system" [19]. The work presented in this paper is based on a novel, multilayered integrated ITS for safety improvement and congestion reduction. The ITS infrastructure is the result of discussions conducted by a group of researchers at the University of Texas at Dallas [3, 25]. Traffic is viewed as a bottom-up phenomenon that is the consequence of individual decisions at the micro-level, and traffic management as a top-down activity that is the result of decisions taken at the macro-level. Both macro and micro-levels consist of multi-agent based infrastructures where autonomous entities continuously communicate and interact with each other. Even though some of the proposed ITS components have already been implemented, the overall infrastructure is still in its conceptual stage.

Given the critical role of interactions among ITS components and their independent decision making capabilities, the use of simulation techniques to test traffic scenarios under nominal and extreme conditions was necessary. MATISSE (**M**ulti-**A**gent based **T**raff**I**c **S**afety **S**imulation syst**E**m) is an agent-based "tailor made" simulation framework that was designed to provide a platform for the execution of such scenarios. The design of this large-scale, distributed, multi-agent based simulation framework revealed the need for the definition of additional entities, adding a layer of complexity to the problem. Before embarking on the full-scale development of MATISSE, the specification and validation of the simulation framework's properties proved to be necessary.

Alloy is a modeling language based on set theory and first order logic that has been used in both industry and academia to validate a wide variety of systems [7, 10, 16]. The language has a simple and concise syntax and comes with a powerful, integrated tool for compiling and analyzing models. The purpose of this paper is to present a formalization of the MATISSE model in Alloy, and discuss how the model's core properties are verified using Alloy's Analyzer. In particular, we discuss an approach to produce execution traces from the specification. These traces serve two purposes: they allow for a thorough analysis and evaluation of the traffic model; and demonstrate the suitability of MATISSE for the simulation of ITS scenarios.

In the following section we give an overview of related works. In Section 3 we briefly present the proposed ITS and MATISSE's high level architecture. In Sections 4 and 5 we discuss how Alloy was used to specify, verify, and analyze MATISSE's model. Finally, in Section 6 we share the lessons learned from this experience.

## 2. TRAFFIC SIMULATION

There are two major approaches to simulate traffic scenarios. Macroscopic models [1, 17] describe traffic as a physical flow of fluid and make use of mathematical equations relating macroscopic quantities (e.g., traffic density, flow rate and average velocity). These models assume rational driving behavior and fairly consistent traffic streams and thus are unfit to model real traffic operations.

In contrast, microscopic models consider the characteristics of individual traffic elements (e.g., vehicles, traffic lights, traffic signals, driver behavior) and their interactions. Typical microscopic models are based on analytical techniques (e.g., queuing analysis, shock-wave analysis) [14] and assume traffic elements with predefined behavioral models. This is a limitation since realistic traffic simulation scenarios call for the modeling of unexpected behavior and unforeseen environmental conditions. The multi-agent paradigm alleviates this

limitation by providing means to address non-deterministic behavior in non-deterministic, unpredictable environments.

Over the last decade, a large number of agent-based traffic simulation systems have been proposed. Some focus on specific small scale traffic problems (e.g., driver behavioral modeling, tactical driving, evacuation management, intersection management) [11, 22, 24] while others attempt to tackle complex large scale traffic scenarios [2, 6, 12]. In this section we restrict our discussion to those that best compare to MATISSE, namely MatSim [2], and Transims [6].

MatSim [2] is an agent-based framework for modeling transport demand. MatSim represents individual travelers as agents endowed with predefined plans. These agents follow a utility based strategy to determine their optimal daily plan. Interactions among agents are implicitly encoded into the agent's utility function. In its current version, traveler agents cannot directly interact with other agents. In addition, agents are not capable of perceiving their environment dynamically. They act upon global environmental knowledge seeded at initialization time.

Similarly, Transims [6] is a large-scale microscopic simulation system for transportation planning and congestion evaluation. In Transims travelers are modeled as agents which can walk, drive cars, or use buses. Traveler agents can decide which plan to select depending on their current state but they cannot dynamically perceive their environment. It is also unclear whether they can interact with other agents. Transims' environment is static and fully observable, thus reducing its capabilities to model complex and realistic scenarios.

Our work enhances the conventional urban traffic simulation by proposing a multi-agent based framework that simulates macro and micro-level traffic entities and their interactions within and across levels. The unique characteristics of MATISSE are: 1) The simulation environment is open, i.e., non-deterministic, dynamic, inaccessible and continuous [23]. The environment has mechanisms that allow the simulation of event propagation. 2) The agents are not given global environmental knowledge to act upon. They dynamically perceive their surroundings through various senses (e.g., vision, hearing, smell). 3) At run-time, the user can change the properties of the simulated agents (e.g, driver "awake" to driver "asleep", disable agent sensors) and the environment (e.g., change the laws that govern the environment) without interrupting the simulation. To the best of our knowledge, no other existing framework offers this feature.

A recent system called JaSim [12] was developed along the same premises as MATISSE. Even though it shares the same environment structure and similar agent perception mechanisms, it lacks the advanced simulation features of event propagation and dynamic property modification discussed above.

# 3. OVERVIEW OF ITS AND MATISSE

In this section, we briefly present the main components of the proposed ITS and discuss MATISSE's architecture. More detailed discussions on these topics can be found in [3, 25, 26].

## 3.1. Elements of a novel ITS

The proposed ITS aims at enforcing communication, interaction, and collaboration between various types of elements defined at various levels of abstraction[1].

The infrastructure is based upon two underlying concepts:

- In order to manage a large environment efficiently, it is necessary to partition the space into smaller defined regions called *traffic area*;
- Each traffic area is assigned a *tower*. A tower is required to: 1) autonomously manage environmental information about its traffic area; 2) be aware of the traffic elements (e.g., vehicles, traffic devices) located in its defined area; 3) be able to interact with local traffic elements to inform them about changes in their surroundings; 4) be able to communicate with other towers to inform them of external events.

In order to manage traffic information efficiently, traffic towers are organized as a hierarchy (see Figure 1). This structure is particularly important for the case when towers need a higher level of knowledge to properly manage their traffic areas. For example, if congestion is caused by an accident in an area, and the micro-level information is insufficient for the tower to determine the best exit route for its local vehicles, it will communicate with a higher level traffic tower to obtain a broader image of the traffic.

The micro-level entities are classified in two categories:

*Mobile Context-Aware Intelligent (CAI) vehicles* [4]. These are vehicles equipped with devices that allow them to 1) monitor the driver's behavior in order to prevent possible accidents; 2) communicate with other vehicles and traffic devices; and 3) interact with the traffic tower infrastructure to obtain traffic information and guidance in real time.

*Stationary Context-Aware Intelligent (CAI) traffic devices*. These include traffic lights, traffic collection devices, and relay units. They serve the purpose of improving safety and traffic flow on roads and highways by providing information about the physical traffic infrastructure and congestion condition. Traffic lights are equipped with adaptive systems that allow them to 1) interact with the traffic tower infrastructure to obtain traffic information in real time, 2) communicate

[1] In the remainder of this paper we will use the word "micro-level" element to refer to an entity that has very limited knowledge of the state of the world. In contrast, a "macro-level" element refers to one that is aware of a larger portion of the world.

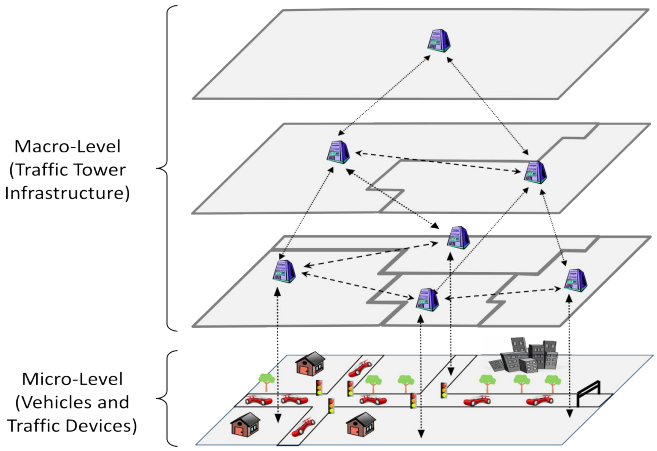


**Figure 1.** ITS super-infrastructure

with vehicles for intersection coordination, and 3) communicate with other traffic light controllers to improve traffic flow when necessary. Traffic collection devices are used on highways (e.g., toll units) to collect information about traffic, and communicate the information to the traffic management system for further analysis (e.g., identification of a drunk driver on the highway). Relay units are used to pass on information between the various communicating entities when the physical distance is too great.

## 3.2. MATISSE Architecture

MATISSE is a "tailor made" multi-agent based simulation platform designed to specify and execute simulation models for the above-mentioned ITS. We define an agent as a software entity which [21]: 1) is driven by a set of tendencies in the form of individual objectives; 2) can communicate, collaborate, coordinate and negotiate with other agents; 3) possesses resources of its own; 4) executes in an environment that is partially perceived; 5) possesses skills and can offer services. A *virtual agent* is an application specific agent that represents a real world concept (e.g., vehicle, traffic device).

MATISSE defines virtual agents for each micro- and macro-level element used in the ITS. *Vehicle agents* simulate the behavior of human drivers, have individual goals (e.g., arriving at some destination in a reasonably short time), influence other agents (e.g., turning signals and changing lanes), and are governed by environmental norms and constraints (e.g., speed limits and traffic signals). *Traffic light* and *traffic collection agents* are aware of and influence nearby vehicles, are able to perceive and adapt to changing conditions, and collaboratively work to achieve certain objectives. Finally, *Traffic Tower agents* autonomously manage and control their traffic area, including the vehicles and traffic devices they enclose.

In addition to these virtual agents, and for software design purposes, it is necessary to introduce two design related concepts: a *cell* is a repository that encompasses all information related to a traffic area. A *cell controller* is a special purpose agent whose main role is to consistently provide virtual agents located within its cell with a correct perception of their surroundings. This is a complex and critical role in any realistic simulation. More information on this topic can be found in [20]. It is important to note that a cell controller does not correspond to a real world concept since real perception is achieved through physical sensors.

*High Level Architecture*

As shown in Figure 2, MATISSE's high level architecture includes three main components: the Agent-Environment System (AES) creates simulation instances; the Data Management System (DMS) stores and processes information collected from the AES; and the Visualization Framework receives information from the DMS and creates 2D or 3D images of the simulation.

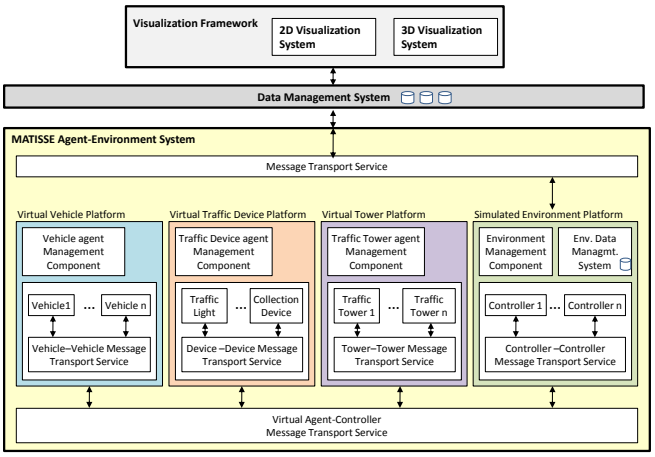


**Figure 2.** Matisse high level architecture

*Matisse's Virtual Agent Platforms*

The four types of agents identified by MATISSE are naturally managed by four distinct agent platforms within the Agent-Environment System (AES) component. The **Virtual Vehicle Platform** manages mobile agents that represent vehicles. Vehicle-agents are created by the *Vehicle-Agent Management Component*, and vehicle-agents communicate with each other through the *Vehicle-Vehicle Message Transport Service*. The **Virtual Traffic Device Platform** manages stationary agents that represent traffic lights, relays and information collection devices. The *Traffic-Device-Agent Management Component* creates and manages traffic-device-agents within the simulation while *Device-Device Message Trans-*

*port Service* handles communication between these stationary traffic-agents. The **Virtual Tower Platform** creates and manages the hierarchical infrastructure of *traffic-tower-agents*. Finally the **Simulated Environment Platform** creates and manages cell controllers. The *Environment Agent Management Component* creates cell controllers, assigns them to a cell, and maintains the cell controller hierarchy for the simulation.

# 4. SPECIFYING MATISSE IN ALLOY

Due to the scale and complexity of the simulation architecture, from a software engineering perspective, we found it necessary to formally specify and validate various simulation properties before starting the implementation of MATISSE. In this section we briefly introduce the Alloy language [15] and present a specification of the simulation properties of MATISSE in Alloy.

## 4.1. Overview of Alloy

In the past two decades, several formalisms have been proposed for multi-agent systems (e.g., temporal logic, multi-modal logic). These formalisms are generally abstract and not related to concrete computational models [9]. Other approaches have used traditional formal languages such as Z and CSP [5, 18]. While providing an accessible notation, these formalisms lack the diagrammatic representation and tool support necessary to effectively analyze models.

Alloy is a specification language based on set theory and first-order relational logic [15]. The language has a simple and concise syntax that can represent complex structural properties and behavior. It comes with an Analyzer, a powerful, integrated tool for compiling and analyzing models. The Analyzer supports two types of automatic analysis: 1) the search for an instance that satisfies all the constraints and relations specified in a model; 2) the identification of a counterexample that violates the assertions specified in a model. Both analysis are performed within a user defined *scope* that bounds the cardinality of entity sets in instances of the model. Outputs can be graphically depicted using the visualizer and evaluated using the command-line evaluator.

Alloy has been used in both industry and academia [7, 10, 16]. Jackson and Vaziri [16] have proposed an approach to verify Java methods in Alloy. At IBM, a subset of Alloy has been used to develop a technique for efficient checking of data structure invariants [10]. Alloy was also used in [8] to test and find bugs in Galileo, a dynamic fault tree analysis tool used at NASA [7].

## 4.2. Specification of MATISSE Static Properties

The static properties of a model describe the conceptual entities and their relationships. In Alloy, these are specified through the *signature* declaration.

For example, **module** `TrafficSimulationEntity`, in Figure 3, specifies vehicle-agents, traffic-light-agents, and tower-agents. It also specifies `VirtualEnvironment`, `TrafficArea`, `Cell` and `CellController`. The **one** keyword constraints the model to one virtual environment. Simulation events (both external and internal) are specified by `Event`.

```
module TrafficSimulationEntity
abstract sig VirtualAgent{}
sig Vehicle extends VirtualAgent{}
sig TrafficLight extends VirtualAgent{}
sig Tower extends VirtualAgent{}
one sig VirtualEnvironment{}
sig TrafficArea{}
sig Cell{}
sig CellController{}
sig Event{}
```

**Figure 3.** Traffic Simulation Entities

Figure 4 shows a partial specification of MATISSE's model. **module** `TrafficSimulation` makes use of the elements defined in **module** `TrafficSimulationEntity` to specify the relations and constrains of the model. An example of a relation, in **sig** `Simulation`, is `guide` that corresponds to the relationship between tower-agents and vehicle-agents. The aggregation of **module** `TrafficSimulationEntity` and `TrafficSimulation` makes up the complete MATISSE simulation model.

```
module TrafficSimulation
open TrafficSimulationEntity
sig Simulation{
  dividedIntoArea: VirtualEnvironment one → TrafficArea,
  control: Tower one → TrafficLight,
  guide: Tower one → Vehicle,
  manage: Tower one → one TrafficArea,
  containTower: TrafficArea one → one Tower,
  containVehicle: TrafficArea one → Vehicle,
  towerCollaborate: Tower → Tower,
  ...
  visionVehicle: CellController one → Vehicle,
  ...
  knows: Vehicle → Event,
  requestVicinity: Vehicle → CellController,
  grantVicinity: CellController → Vehicle → Vehicle
  sendEvent: Vehicle → Event → Tower,
  notifyEvent: Tower → Event → Vehicle,
  propagateEvent: Tower → Event → Tower
}{
  containTower = ~manage
  containVehicle = containTower·guide
  cellContainVehicle = cellContainCC·visionVehicle
  vehicleInfluence = ~visionVehicle
  (sendEvent·Tower) in knows
  (sendEvent·Tower)·(Vehicle·sendEvent) in ~guide
  ...
}
```

**Figure 4.** Partial Specification of MATISSE's Model

Alloy enables the precise specification of static properties such as "each *virtual traffic area* is assigned a *tower-agent*". Using relation multiplicities, `containTower:`

`TrafficArea` **one** → **one** `Tower` specifies a one-to-one relation between traffic area and tower elements. Further, the constraint `containTower`= ~`manage` ensures that each tower-agent is assigned to a unique traffic area, and that each area is uniquely associated to its tower-agent.

## 4.3. Specification of MATISSE Dynamic Properties

In Alloy, operations are specified through *predicates*, which relate valid instances of `Simulation` through a change in its composition. For instance, **pred** `requestCCVicinity` adds the relation between a vehicle and its cell controller to `s` in order to produce `s'`, in which `s` and `s'` denote the before and after states of `Simulation`.

```
pred requestCCVicinity[vc: Vehicle→ CellController,
s, s':Simulation]{
  vc in ~(Simulation·visionVehicle)
  s'·requestVicinity = s·requestVicinity + vc
}
```

Thus far, the presented specification produces unrelated instances of the MATISSE simulation model. This is not sufficient for modeling simulation scenarios where a sequence of operations relating different instances of `Simulation` is required. As such, we extend our model with *execution traces* to allow the ordered execution of operations. To produce execution traces, we specify a linear ordering over `Simulation` elements (see Figure 5).

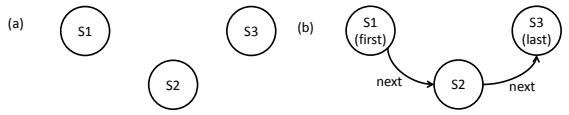


**Figure 5.** (a) Unrelated instances of the model (b) Execution trace of the model

This is achieved by importing the library module `util/ordering`. This module includes functions `first`, `next`, and `last`. As depicted by Figure 5 (b), `first` returns the first element *S*1, `s1.next` returns *S*2 and `s2.next` returns *S*3, and `last` returns the last element *S*3.

The following fragments of MATISSE's specification illustrate the new constraints added to the model to enable execution traces. The **pred** `init` defines the initial conditions (i.e., the initial composition) and **pred** `inv` defines invariants (i.e., properties that never change during an execution trace) of `Simulation`. Any adjacent `Simulation` in the ordering is related by **fact** `traces`. For instance, if a vehicle requests its vicinity in `s`, then the vehicle's vicinity will be granted in `s'` through operation `grantVehicleVicinity`.

```
module TrafficSimulation
open util/ordering[Simulation] as t
…
pred init[s:Simulation]{ …}
pred inv[s, s':Simulation]{
  s'·dividedIntoArea = s·dividedIntoArea
  s'·containTower = s·containTower
  …
}
fact traces {
  init[first]
  all s:Simulation - last | let s' = s·next {
    inv[s,s']
    …
    (#s·knows ≠ 0 and #s·requestVicinity ≠ 0
    and #s·grantVicinity = 0) ⇒ {
      s'·knows = s·knows
      s'·requestVicinity = s·requestVicinity

      let v = (s·requestVicinity)·CellController | {
        ((v in (s·requestVicinity)·CellController) and
          (v not in Vehicle·(CellController·(s·grantVicinity))))
          ⇒ {let x = (cellControllers[v,Simulation]→Vehicle)
            & (CellController→ vicinityVV[v,Simulation]) |
              grantVehicleVicinity[flip23[x],s,s']}
        else s'·grantVicinity = s·grantVicinity
      }
    }
    …
}
```

With this specification, it is possible to analyze the static and dynamic properties of MATISSE. In addition, a number of ITS traffic scenarios involving collaboration, information dissemination, and event propagation can be planned and designed to validate MATISSE's traffic model.

# 5. ANALYZING MATISSE'S PROPERTIES

In this section, we show how the above-discussed Alloy models can be analyzed to ensure the consistency of the specification and satisfaction of MATISSE's traffic model properties. Hereafter, we refer to the consistency checking of the Alloy specification as *verification*, and reserve the term *validation* to the activity of ensuring that the specified model copes with the intended high level requirements of MATISSE.

## 5.1. MATISSE's Properties Verification

For the purposes of verification, the Alloy Analyzer is used to find instances that violate the assertions specified in the model. In particular, we show how static and dynamic properties of the MATISSE simulation model can be verified using Alloy, thus ensuring the necessary rigor to analyze the specification against design flaws.

The assertion `VehicleSendEventOnlyToTowerGuiding` states that for all instances of the `Simulation` a vehicle can send an event (through relation `sendEvent`) only to the tower guiding it. No counterexample is found for this static property following the constraining fact `(sendEvent.Tower).(Vehicle.sendEvent) in` ~`guide` specified in `Simulation`.

```
assert VehicleSendEventOnlyToTowerGuiding{
  all s: Simulation{
    let v = ((s·sendEvent)·Tower)·Event |
       (v ≠ none) implies
       Event·(v·(s·sendEvent)) = (s·guide)·v
  }
}
```

The assertion `RequestIsGranted` is an example of verification of a dynamic property of the model, in which we ensure consistency between adjacent instances of `Simulation`. It states that if a vehicle makes a request for vicinity in `s`, then the request must be granted in `s'`. No counterexample is found for this property.

```
assert RequestIsGranted{
  all s:Simulation-last, s':s.next |
    let v = (s.requestVicinity).CellController |
      ((v - Vehicle.(CellController.(s.grantVicinity)))
      ≠ none) ⇒
        v in Vehicle.(CellController.(s'.grantVicinity))
}
```

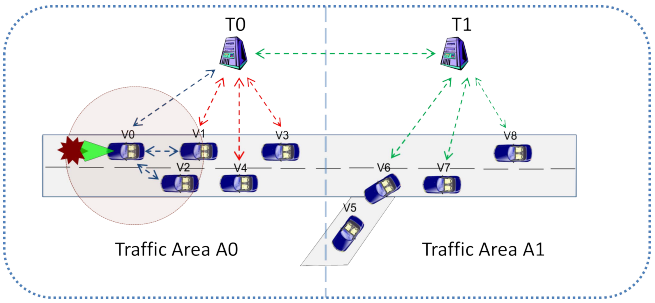


**Figure 6.** Scenario for safety enhancement and congestion reduction

## 5.2. Traffic Scenario Description

The scenario depicted in Figure 6 demonstrates the suitability of MATISSE for safety improvement and congestion reduction. This ITS scenario consists of vehicles driving on a one-way road. An event (e.g., an accident, an obstruction on the road, or any other abnormal condition) has occurred in Traffic Area A0, and vehicle V0 perceives the event within its field of vision (shown as a green cone). Under this scenario, V0 takes the following steps: 1) Informs all vehicles located in its *close vicinity* [2] (shown as a circle) about the perceived event via *vehicle-to-vehicle* interactions. The notified vehicles are able to take the necessary actions to avoid a major accident. 2) Informs traffic tower T0 about the perceived event via *vehicle-to-infrastructure* interactions.

After deliberation and based on the event characteristics, T0 alerts the vehicles located in A0 under its control (i.e., V1 to V4) about the event (to enhance safety). T0 also determines the potential impact of this event on to neighboring traffic areas and informs the adjacent traffic tower T1 of the event. T1 deliberates, and informs all vehicles located within Traffic Area A1 of the event and guides them in their choice of the best alternate route to follow (to avoid congestion). All vehicles in the traffic area make use of the broader traffic information to improve the overall safety condition and avoid traffic congestion.

## 5.3. Traffic Scenario Validation

The execution traces generated from the Alloy models validate the specified MATISSE's properties (i.e., virtual agent perception, agent-to-agent interaction, and event propagation) with respect to the above-described traffic scenario. Additionally, these traces highlight how safety improvement and congestion reduction goals are achieved in MATISSE.

The execution of the model produces the execution trace consisting of the following sets of elements:

[2] A vehicle's vicinity represents the vehicles that are positioned within the vehicle's range of communication, determined by the available communication technology [27].

```
this/Simulation = {Simulation0, Simulation1,
    Simulation2, Simulation3, Simulation4}
t/Vehicle = {t/Vehicle0, t/Vehicle1, t/Vehicle2,
    t/Vehicle3, t/Vehicle4, t/Vehicle5, t/Vehicle6,
    t/Vehicle7, t/Vehicle8}
t/Tower = {t/Tower0, t/Tower1}
t/TrafficArea = {t/TrafficArea0, t/TrafficArea1}
t/CellController = {t/CellController0}
t/Event = {t/Event0}
```

These sets (e.g., **sig** `Vehicle`, **sig** `Tower`) correspond to the signatures defined in the specification and the elements (e.g., $t/Vehicle0$, $t/Tower0$) are arbitrarily assigned to the sets at execution time. For the purpose of this section, sets such as `VirtualEnvironment` and `Cell` are omitted from the discussion.

Figure 7 shows a visual representation of the last instance of the execution trace (i.e., *Simulation*4). Each element is depicted as a geometric figure, and each relation (e.g., *knows*, *requestVicinity*) as an arrow. The visual representation of the initial and intermediate instances of the trace (i.e., *Simulation*0, *Simulation*1, *Simulation*2, and *Simulation*3) are omitted due to space limitation. The following steps describe in detail the complete execution trace.

In *Simulation*0, *Vehicle*0 perceives an *Event* through its sensors. It stores this information into its knowledge base as reflected by relation *knows*. In *Simulation*1, *Vehicle*0 requests the identities of the vehicles in its vicinity from the *CellController*, and communicates the event information to its virtual traffic tower. This is reflected by relation *requestVicinity* between *Vehicle*0 and *CellController*, and relation $sendEvent[Event]$ between *Vehicle*0 and *Tower*0. *Tower*0 stores the event information into its knowledge base as reflected by relation *towerKnows* and relation *vehicleCollaborate* denotes the vehicles in a vehicle's vicinity.

In *Simulation*2, the *CellController* proceeds by sending the *Vehicle*1 and *Vehicle*2's ids to *Vehicle*0. This is represented by relations $grantVicinity[Vehicle1]$ and $grantVicinity[Vehicle2]$. *Tower*0 communicates *Event* to all vehicles in its traffic area. This is depicted by relations $notifyEvent[Event]$. Also, *Tower*0 uses its acquaintance model represented by relation *towerCollaborate* to identify

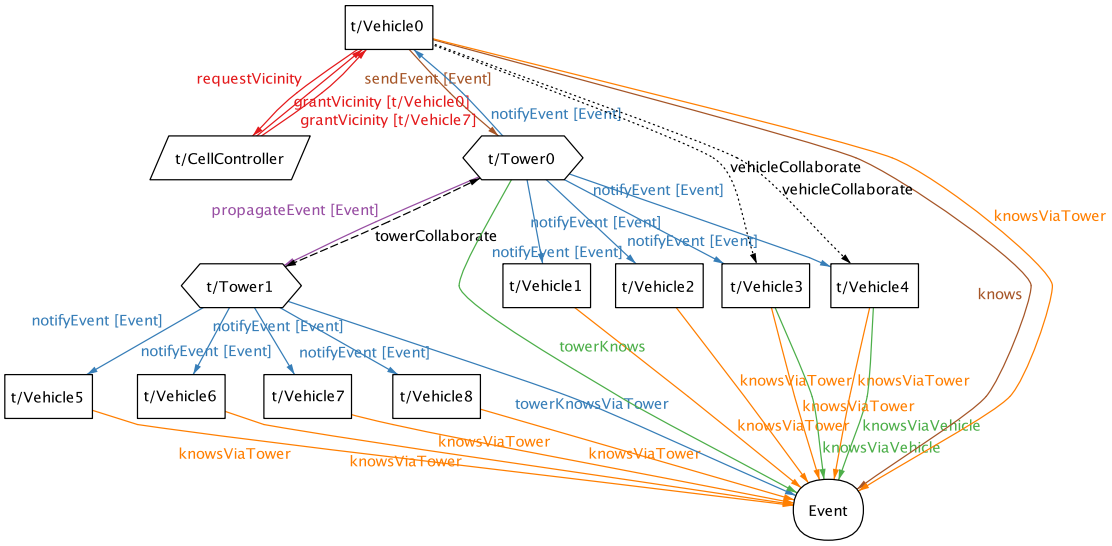


**Figure 7.** Last instance of the execution trace

the neighboring tower that might be affected by the event (in this case *Tower*1) and passes *Event* on to it. This is reflected by relation $propagateEvent[Event]$. Upon receiving this information, *Tower*1 stores *Event* into its knowledge base as reflected by relation *towerKnowsViaTower*.

In *Simulation*3, *Vehicle*0 communicates the *Event* to *Vehicle*1 and *Vehicle*2 which, in turn store the information into their knowledge bases as reflected by the *knowsViaVehicle* relations. Upon receiving the event information, all vehicles within *Tower*0's traffic area store the event information into their knowledge bases as reflected by the *knowsViaTower* relation. Also, *Tower*1 communicates *Event* to its local vehicles as represented by relation $notifyEvent[Event]$.

Finally, in *Simulation*4, all vehicles within *Tower*1's traffic area (*Vehicle*5, *Vehicle*6, *Vehicle*7, and *Vehicle*8) store the event information received into their knowledge base. This is reflected by the relation *knowsViaTower*.

## 6. LESSONS LEARNED

The lessons learned by specifying and executing MATISSE's model in Alloy are summarized in the points given bellow:

*Abstraction.* By abstracting from implementation details, Alloy helped us focus on the most important aspects of system design and explore design alternatives. For instance, it allowed us to revisit various responsibilities assigned to agents when modeling agent-to-agent interactions (e.g., collaboration between vehicles and traffic towers, event propagation across traffic areas).

*Process.* We have started the design activity with a small model containing just a few signatures and constraints, and progressed by adding detail iteratively. At each step, key aspects of the system were modeled, checked, and simulated without writing a single line of code.

*Model Execution.* The execution of traces is a valuable tool that allowed us to identify several conceptual inconsistencies of the model. The step-by-step scenario execution enabled us to analyze the various states in which the traffic model can be and validate its high level properties.

However, we experienced difficulty coping with the timing aspects of the simulation. For instance, there is no built in mechanism in Alloy to specify and verify real-time properties such as that a given communication among agents occurs in due time. Although Alloy includes some basic temporal constraints, it is less expressive than traditional temporal logics for specifying more complex temporal properties. In addition, when specifying behavioral constraints to ensure consistency between adjacent instances of execution traces, we need to exert caution not to over-constrain the model. In this respect, obtaining specific execution traces to validate traffic scenarios can be difficult. Finally, despite its apparent simplicity, a strong foundation in set theory and logic is essential to specify complex interactions involving communication and cooperation among agents in Alloy.

Based on these observations, we believe that an approach combining Alloy and Statecharts [13] can alleviate these limitations, allowing for the incorporation of real-time constraints while contributing to a more natural representation of behavioral properties. Furthermore, this extended formalism could help with the modeling and analysis of concurrent behavior.

## 7. CONCLUSIONS

MATISSE is a multi-agent based simulation platform designed to specify and execute traffic simulations for a new generation of ITS. MATISSE's unique features include its open, decentralized and distributed environment; the ability of agents to perceive their surroundings in simulated real time; and the ability to execute micro- and macro-level ITS scenarios within the same framework.

In this paper we discussed how Alloy was used to specify and analyze the static and dynamic properties of such a complex simulation system, and shared the lessons learned from this experience. Future work includes determining how to integrate Alloy models with state-charts to incorporate real-time constraints and obtain a more natural representation of behavioral properties, as well as to evaluate the scalability of the Alloy specification for more complex interaction patterns.

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