

6.4 & 6.5 Practice

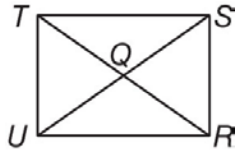
Example 1: Quadrilateral $RUTS$ below is a rectangle. If $US = 6x + 3$ and $RT = 7x - 2$, find x .

The diagonals of a rectangle are congruent, so $US = RT$.

$$6x + 3 = 7x - 2$$

$$3 = x - 2$$

$$5 = x$$



Example 2: Quadrilateral $RUTS$ below is a rectangle. If $m\angle STR = 8x + 3$ and $m\angle UTR = 16x - 9$, find $m\angle STR$.

$\angle UTS$ is a right angle, so $m\angle STR + m\angle UTR = 90^\circ$.

$$8x + 3 + 16x - 9 = 90$$

$$24x - 6 = 90$$

$$24x = 96$$

$$x = 4$$

$$m\angle STR = 8x + 3 = 8(4) + 3 \text{ or } 35^\circ$$

You try!!

Quadrilateral $ABCD$ is a rectangle.

1. If $AE = 36$ and $CE = 2x - 4$, find x .

$$2x - 4 = 36$$

$$2x = 40$$

$$x = 20$$

2. If $BE = 6y + 2$ and $CE = 4y + 6$, find y .

$$6y + 2 = 4y + 6$$

$$2y = 4$$

$$y = 2$$

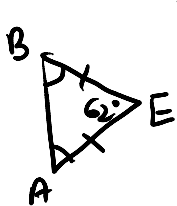
3. If $BC = 24$ and $AD = 5y - 1$, find y .

$$5y - 1 = 24$$

$$5y = 25$$

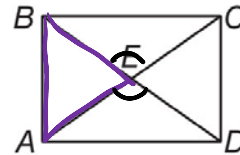
$$y = 5$$

4. If $m\angle BEA = 62^\circ$, find $m\angle BAC$.



$$\begin{array}{r} 180 \\ - 62 \\ \hline 118 \end{array}$$

$$\frac{118}{2} = 59^\circ$$



5. If $m\angle AED = (12x)^\circ$ and $m\angle BEC = (10x + 20)^\circ$, find $m\angle AED$.

vertical angles

$$12x = 10x + 20$$

$$2x = 20$$

$$x = 10$$

$$m\angle AED = 12(10) = 120^\circ$$

6. If $BD = 8y - 4$ and $AC = 7y + 3$, find BD .

$$8y - 4 = 7y + 3$$

$$y = 7$$

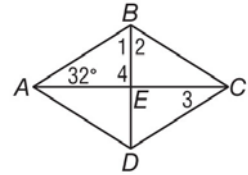
$$BD = 8(7) - 4 = 56 - 4 = 52$$

Example: In rhombus $ABCD$, $m\angle BAC = 32^\circ$. Find the measure of each numbered angle.

$ABCD$ is a rhombus, so the diagonals are perpendicular and $\triangle ABE$ is a right triangle.

Thus $m\angle 4 = 90^\circ$ and $m\angle 1 = 90 - 32$ or 58° . The diagonals in a rhombus bisect the vertex angles, so $m\angle 1 = m\angle 2$. Thus, $m\angle 2 = 58^\circ$.

A rhombus is a parallelogram, so both pairs of opposite sides are parallel. $\angle BAC$ and $\angle 3$ are alternate interior angles for parallel lines, so $m\angle 3 = 32^\circ$.



You try!!

Quadrilateral $ABCD$ is a rhombus. Find each value or measure.

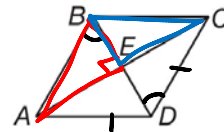
1. If $m\angle ABD = 60^\circ$, find $m\angle BDC$.

60°

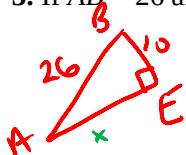
if 11 lines, then
alt. int. $\angle$ s $\cong$

2. If $AE = 8$, find AC .

$16u$



3. If $AB = 26$ and $BD = 20$, find AE .



$$\begin{aligned} 10^2 + x^2 &= 26^2 \\ 100 + x^2 &= 676 \\ x^2 &= 576 \end{aligned}$$

$24u$

4. Find $m\angle CEB$.

90°

diagonals $\perp$

5. If $m\angle CBD = 58^\circ$, find $m\angle ACB$.



$$\begin{aligned} 180 \\ - 90 \\ - 58 \\ \hline 32^\circ \end{aligned}$$

6. If $AE = 3x - 1$ and $AC = 16$, find x .

$$\begin{aligned} 2(3x - 1) &= 16 \\ 6x - 2 &= 16 \\ 6x &= 18 \\ x &= 3u \end{aligned}$$

7. If $AD = 2x + 4$ and $CD = 4x - 4$, find x .

$$4x - 4 = 2x + 4$$

$$2x = 8$$

$$x = 4u$$

8. If $m\angle BAE = (3x + 12)^\circ$ and $m\angle DAE = (5x - 2)^\circ$, find x .

$$5x - 2 = 3x + 12$$

$$2x = 14$$

$$x = 7^\circ$$

Diagonals bisect
opp. $\angle$ s

Quadrilateral $QRST$ is a square. Find each value or measure.

1. If $m\angle TQR = (8n + 8)^\circ$, find n .

$$8n + 8 = 90$$

$$8n = 82$$

$$n = 10.25^\circ$$

