

# Drawing Finite State Machines in L<sup>A</sup>T<sub>E</sub>X and TikZ

## A Tutorial

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### 1 Introduction

“L<sup>A</sup>T<sub>E</sub>X (pronounced lay-tek) is an open-source, multiplatform document preparation system for producing professional-looking documents. . . It is particularly suited to producing long, structured documents, and is very good at typesetting equations” [University of Edinburgh Information Services, 2014].

The capabilities of the system are greatly enhanced with the help of native and third-party packages.<sup>1</sup> TikZ<sup>2</sup> is a package for drawing all kinds of graphics.

This tutorial introduces the reader to L<sup>A</sup>T<sub>E</sub>X and the TikZ package, particularly for drawing state diagrams of finite automata.

### 2 Setting up L<sup>A</sup>T<sub>E</sub>X

To proceed with the tutorial, a working L<sup>A</sup>T<sub>E</sub>X setup is necessary. You may install it locally on your machine, but the simplest thing to do is use ShareL<sup>A</sup>T<sub>E</sub>X ([sharelatex.com](http://sharelatex.com)). If you sign up using your nd.edu address, you’ll get unlimited private project. For further information regarding setup, visit <http://www.latex-project.org/get/>.

### 3 The preamble

Every L<sup>A</sup>T<sub>E</sub>X document starts with a *preamble*. To make our automata look like the ones in the textbook [Sipser, 2012], use the following preamble:

```
\documentclass{article}      % What kind of document this is
\usepackage{tikz}           % Import the tikz package
\usetikzlibrary{automata}   % Import library for drawing automata
\usetikzlibrary{positioning} % ...positioning nodes
\usetikzlibrary{arrows}     % ...customizing arrows
\tikzset{node distance=2.5cm, % Minimum distance between two nodes. Change if necessary.
  every state/.style={ % Sets the properties for each state
    semithick,
    fill=gray!10},
  initial text={},          % No label on start arrow
  double distance=2pt,     % Adjust appearance of accept states
  every edge/.style={ % Sets the properties for each transition
```

<sup>1</sup>The Comprehensive T<sub>E</sub>X Archive Network (CTAN) is the central place for all kinds of material around T<sub>E</sub>X. <https://www.ctan.org/?lang=en>

<sup>2</sup><https://www.ctan.org/pkg/pgf?lang=en>

```

draw,
->,>=stealth',      % Makes edges directed with bold arrowheads
auto,
semithick}}
\let\epsilon\varepsilon

```

After the preamble comes the content:

```

\begin{document}
% Content goes here
\end{document}

```

## 4 Basics

While there are many tutorials online, I suggest two: University of Edinburgh Information Services [2014] and <https://www.latex-tutorial.com/>.

Here are some symbols often used in this course:

symbol	control sequence	usual meaning
$\Sigma$	<code>\Sigma</code>	alphabet
$\Gamma$	<code>\Gamma</code>	another alphabet
$\varepsilon$	<code>\varepsilon</code>	empty string
$\circ$	<code>\circ</code>	concatenation
$\#$	<code>\texttt{\#}</code>	marker symbol
$\$$	<code>\texttt{\\$}</code>	marker symbol
$\_$	<code>\textvisiblespace</code>	blank symbol
$\{ \}$	<code>\{ \}</code>	delimiters for sets
$\emptyset$	<code>\emptyset</code>	empty set
$\neq$	<code>\neq</code>	is not equal to
$\in$	<code>\in</code>	is an element of
$\notin$	<code>\notin</code>	is not an element of
$\subseteq$	<code>\subseteq</code>	is a subset of
$\rightarrow$	<code>\rightarrow</code>	(various meanings)
$\delta$	<code>\delta</code>	transition function
$\alpha$	<code>\alpha</code>	regular expression
$*$	<code>\ast</code>	Kleene star

## 5 Drawing automata

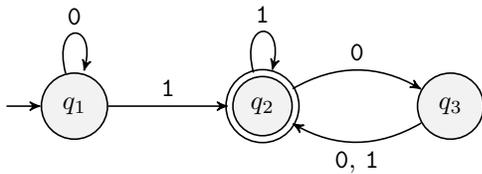
Let's start off with a simple DFA from Sipser [2012] (Figure 1.6). The formal description of the DFA is:

$$M_1 = (\{q_1, q_2, q_3\}, \{0, 1\}, \delta, q_1, \{q_2\}),$$

where  $\delta$  is given by:

	0	1
$q_1$	$q_1$	$q_2$
$q_2$	$q_3$	$q_2$
$q_3$	$q_2$	$q_2$

Below is the code that generates the state diagram of  $M_1$ .



```
\begin{tikzpicture}
  \node[state, initial] (q1) {$q_1$};
  \node[state, accepting, right of=q1] (q2) {$q_2$};
  \node[state, right of=q2] (q3) {$q_3$};
  \draw (q1) edge[loop above] node {\tt 0} (q1);
  \draw (q1) edge node {\tt 1} (q2);
  \draw (q2) edge[loop above] node {\tt 1} (q2);
  \draw (q2) edge[bend left] node {\tt 0} (q3);
  \draw (q3) edge[bend left] node {\tt 0}, {\tt 1} (q2);
\end{tikzpicture}
```

Below, we'll go through this example piece by piece.

## 5.1 The tikzpicture environment

Inside the document, each TikZ diagram must reside in a `tikzpicture` environment:

```
\begin{tikzpicture}
% tikz code goes here
\end{tikzpicture}
```

## 5.2 Nodes

Let's start off by drawing the nodes. Nodes can be positioned either manually or relative to other nodes. Relative placement is often much easier.



```
\begin{tikzpicture}
  \node[state, initial] (q1) {$q_1$};
  \node[state, accepting, right of=q1] (q2) {$q_2$};
  \node[state, right of=q2] (q3) {$q_3$};
\end{tikzpicture}
```

The general form of the `\node` command is:

```
\node[<options>] (<name>) at (<x>,<y>) {<label>};
```

The `<options>`, `(<name>)`, and `at (<x>,<y>)` are all optional, but the `{<label>}` is required.

**Options** The options (for finite automata) are:

- **state**: always give this option to draw a node as a state
- **initial**: specifies the start state
- **accepting**: specifies an accept state

Note that the size of a node depends on the length of its label; to force a minimum size (say, 1 inch), use `minimum size=1in`.

**Name** The name of a node is the name by which you refer to the node, when positioning other nodes relative to it or when drawing edges into or out of it.

**Position** You specify the absolute position of a node using `at (<x>,<y>)` where `<x>` and `<y>` are coordinates (`<x>` coordinates go to the right; `<y>` coordinates go up).

Or you can specify a relative position using `left of=<name>`, `right of=<name>`, `above of=<name>`, `below of=<name>`. There's also `above left of=<name>`, etc.<sup>3</sup>

The `positioning` library which we have already imported provides some further options.

- `xshift=x`, `yshift=y`: Gives manual control of the node positions after relative placement. Eg:

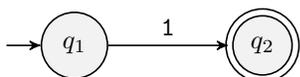
```
\node[state, right of=q1, xshift=1cm] (q2) {$q_2$};
```

**Label** This can be anything you want. Typically you will surround it with dollar signs to use math mode.

### 5.3 Edges

Once the states are all in place, let's start adding the transitions, that is, the edges between the states.

The `\draw` command can be used to draw the edges between the already created nodes (states).



```
\begin{tikzpicture}
\node[state, initial] (q1) {$q_1$};
\node[state, accepting, right of=q1] (q2) {$q_2$};
\node[state, right of=q2] (q3) {$q_3$};
\draw (q1) edge node {\tt 1} (q2);
\end{tikzpicture}
```

The general syntax is as follows:

```
\draw (<source node>) edge[<options>] node {<label>} (<dest node>);
```

**Source and destination nodes** Note that `<source node>` and `<dest node>` are the names of the nodes, not their labels.

**Options** The `<options>` modify the appearance of the edge.

- For edges that start and end in the same node (self-loops), you must use `loop above`, `loop below`, `loop left`, or `loop right`.
- By default, the edges are straight, so to prevent overlaps use `bend left` or `bend right`.
- To modify the placement of the edge label, use `above` or `below`.

**Label** This can be anything you want. Note that Sipser uses typewriter font for symbols, so you probably want to write `{\tt 0}` or `\texttt{0}`.

**Shorthand** Multiple edges can be drawn with the same `draw` command, like so:

```
\draw (q1) edge[loop above] node {\tt 0} (q1)
edge node {\tt 1} (q2)
\draw (q2) edge[loop above] node {\tt 1} (q2)
edge[bend left] node {\tt 0} (q3)
\draw (q3) edge[bend left] node {{\tt 0}, {\tt 1}} (q2);
```

<sup>3</sup>Technically, these options are deprecated, but we find them useful anyway. See <https://tex.stackexchange.com/questions/9386/difference-between-right-of-and-right-of-in-pgf-tikz>.

## 6 More examples

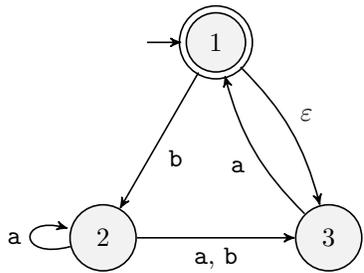
As another example, let's draw a NFA (Sipser, Figure 1.42).

$$N_1 = (\{1, 2, 3\}, \{a, b\}, \delta, 1, \{1\}),$$

where  $\delta$  is given by:

	a	b	$\epsilon$
1	$\{\}$	$\{2\}$	$\{3\}$
2	$\{2, 3\}$	$\{3\}$	$\{\}$
3	$\{1\}$	$\{\}$	$\{\}$

Below is the code that generates the state diagram of  $N_1$ .



```
\begin{tikzpicture}
\node[state, initial, accepting] (1) at (1.5,2.6) {$1$};
\node[state] (2) at (0,0) {$2$};
\node[state] (3) at (3,0) {$3$};

\draw (1) edge node{\tt b} (2)
      edge[bend left=15] node {$\epsilon$} (3)
      (2) edge[loop left] node{\tt a} (2)
      edge[below] node{{\tt a}, {\tt b}} (3)
      (3) edge[bend left=15] node{\tt a} (1);
\end{tikzpicture}
```

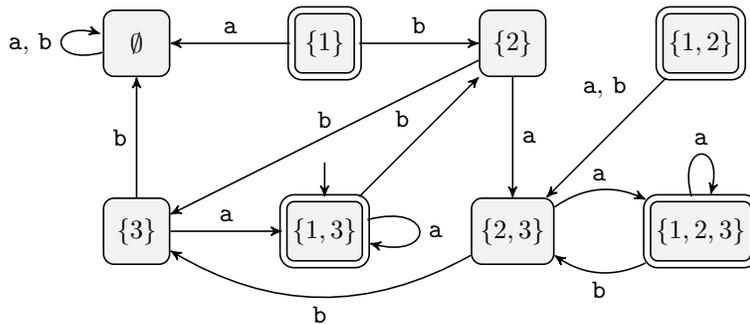
Our final example is the state diagram of the DFA equivalent to the NFA  $N_1$ :

$$D_2 = (\{\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}, \{a, b\}, \delta, \{1, 3\}, \{\{1\}, \{1, 2\}, \{1, 3\}, \{1, 2, 3\}\}),$$

where  $\delta$  is given by

	a	b
$\emptyset$	$\emptyset$	$\emptyset$
$\{1\}$	$\emptyset$	$\{2\}$
$\{2\}$	$\{2, 3\}$	$\{3\}$
$\{3\}$	$\{1, 3\}$	$\emptyset$
$\{1, 2\}$	$\{2, 3\}$	$\{2, 3\}$
$\{1, 3\}$	$\{1, 3\}$	$\{2\}$
$\{2, 3\}$	$\{1, 2, 3\}$	$\{3\}$
$\{1, 2, 3\}$	$\{1, 2, 3\}$	$\{2, 3\}$

Below is the code that generates the state diagram.



```

\begin{tikzpicture}
  \tikzset{every state/.append style={rectangle, rounded corners}}
  \node[state] (emp) {$\emptyset$};
  \node[state, accepting, right of=emp] (1) {$\{1\}$};
  \node[state, right of=1] (2) {$\{2\}$};
  \node[state, accepting, right of=2] (12) {$\{1, 2\}$};
  \node[state, below of=emp] (3) {$\{3\}$};
  \node[state, initial, initial where=above, accepting, right of=3] (13) {$\{1, 3\}$};
  \node[state, right of=13] (23) {$\{2, 3\}$};
  \node[state, accepting, right of=23] (123) {$\{1, 2, 3\}$};

  \draw (emp) edge[loop left] node {\tt a}, {\tt b} (emp)
    (1) edge[above] node {\tt a} (emp)
    (1) edge node {\tt b} (2)
    (2) edge node {\tt a} (23)
    (2) edge[above] node {\tt b} (3)
    (12) edge[auto=right,near start] node {\tt a}, {\tt b} (23)
    (3) edge node {\tt b} (emp)
    (3) edge node {\tt a} (13)
    (13) edge[loop right] node {\tt a} (13)
    (13) edge node {\tt b} (2)
    (23) edge[bend left,above] node {\tt a} (123)
    (23) edge[bend left] node {\tt b} (3)
    (123) edge[loop above] node {\tt a} (123)
    (123) edge[bend left,below] node {\tt b} (23);
\end{tikzpicture}

```

## References

Michael Sipser. *Introduction to the Theory of Computation*. Cengage Learning, 3rd edition, 2012.

University of Edinburgh Information Services. *LaTeX for beginners*. <http://www.docs.is.ed.ac.uk/skills/documents/3722/3722-2014.pdf>, 2014.