

VOLUME

I

COMPUTER AND ROBOT VISION

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Robot Vision is an impressive book....an excellent introduction to the field and the first book to thoroughly cover the mathematics of computer vision. Charles Thorpe. American Scientist. A very good book indeed, probably the best currently available on robot vision and related topics....a valuable reference work for researchers in this field. T.M. Husband.Â Robot Vision presents a coherent development, from image formation, through image analysis to scene analysis. The remarkable achievement of this book is that it serves both as a personal statement of the Horn school of vision and as a textbook. Every scientist and engineer involved with computational vision should read it, carefully! Alan K. Mackworth. Professor, University of British Columbia.