

# College Algebra Formulas and Rules

Standard Form (Linear)

$$Ax + By = C$$

Point-Slope Formula

$$y - y_1 = m(x - x_1)$$

Slope-Intercept Form

$$y = mx + b$$

Slope Formula

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Distance Formula

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Midpoint Formula

$$\left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

General Form (Quadratic)

$$ax^2 + bx + c = y \text{ or } f(x) = ax^2 + bx + c; f(x) \equiv y$$

Standard (Vertex) Form

$$f(x) = a(x - h)^2 + k$$

Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Vertex of a Parabola

$$(h, k) = \left( \frac{-b}{2a}, f\left(\frac{-b}{2a}\right) \right) \text{ or } \left( \frac{-b}{2a}, c - \frac{b^2}{4a} \right)$$

Equation of a Circle

$$r^2 = (x - h)^2 + (y - k)^2$$

$$r = \sqrt{(x - h)^2 + (y - k)^2}$$

$r$  = radius,  $(h, k)$  = center of circle

Difference of Squares

$$(x^2 - y^2) = (x - y)(x + y)$$

Sum of Squares

$$x^2 + y^2; \text{ prime}$$

Perfect Square Trinomial

$$x^2 + 2xy + y^2 = (x + y)^2$$

$$x^2 - 2xy + y^2 = (x - y)^2$$

Difference of Cubes

$$x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

Sum of Cubes

$$x^3 + y^3 = (x + y)(x^2 - xy + y^2)$$

▲ Tip: Use S.O.A.P. to remember the signs in the Diff. and Sum of Cubes formulas—Same, Opposite, Always Positive.

$$x^0 = 1$$

$0^0 = \text{undef.}$

$$\left( \frac{x^z}{y^z} \right)^n = \frac{x^{zn}}{y^{zn}}$$

$y \neq 0$

$$x^{-n} = \frac{1}{x^n}$$

$x \neq 0$

$$(x^z)^n = x^{zn}$$

$$(xy)^z = x^z y^z$$

$$\frac{x^n}{x^z} = x^{n-z}$$

$x \neq 0$

$$x^z x^n = x^{z+n}$$

## Exponent Properties



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<http://www.lsco.edu/learningcenter/math.asp>

$$\sqrt[n]{x} = x^{1/n}; n \neq 0$$

$$(\sqrt[n]{x})^z = \sqrt[n]{x^z} = x^{z/n}$$

$$x^n + x^n = 2x^n$$

$$2x^n - x^n = x^n$$

$$\sqrt{\frac{x}{y}} = \frac{\sqrt{x}}{\sqrt{y}}; y \neq 0$$



## Log Properties

$$y = \log_b x \Leftrightarrow b^y = x$$

$$\log_b 1 = 0; \log_b 0 = \text{undef.}$$

$$\log_b b^x = x$$

$$\log_b y = \frac{\log_a y}{\log_a b}$$

► Tip: Use the change of base formula to convert to base 10 (log) or base e (ln). Some calculators handle only these bases.

$$\log_b b = 1$$

$$b^{\log_b x} = x$$

$$\log_b M^p = p \log_b M$$

$$\log_b x = \log_b y \rightarrow x = y$$

$$\log_b MN = \log_b M + \log_b N$$

$$\log_b \frac{M}{N} = \log_b M - \log_b N$$