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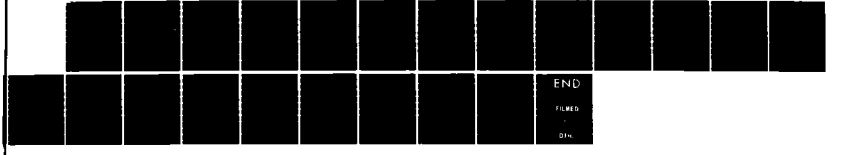

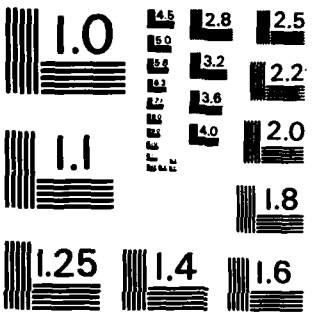

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Concurrent Programming Using Actors: Exploiting Large-Scale Parallelism

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Abstract

We argue that the ability to model shared objects with changing local states, dynamic reconfigurability, and inherent parallelism are desirable properties of any model of concurrency. The *actor model* addresses these issues in a uniform framework. This paper briefly describes the concurrent programming language *Act3* and the principles that have guided its development. *Act3* advances the state of the art in programming languages by combining the advantages of object-oriented programming with those of functional programming. We also discuss considerations relevant to large-scale parallelism in the context of *open systems*, and define an abstract model which establishes the equivalence of systems defined by actor programs.

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We argue that the abilty to modle shaared objects with changing local states dynamic reconfigurabilty, and inherent parellism are desirable properties of any model of concurrency. The actor model addresses these issues in a uniform framework. This paper briefly describes the concurrent programming language Act3 and the principles that have guided its development. Act3 advances the state of theart inprogramming languages by combining the advantages of object-oriented programming with those of functional programming. We also discuss considerations revelant to the large scale parellism in the

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1 Background

The theory of concurrent programming languages has been an exciting area of research in the last decade. Although no consensus has emerged on a single model of concurrency, many advances have been made in the development of various contending models. There have also been some consistent paradigm shifts in the approach to concurrency; an interesting discussion of such paradigm shifts may be found in [Pratt 83].

The actor model of computation has developed contemporaneously in the last decade along with other models based on Petri Nets, the λ-calculus, and communicating sequential processes. There has been a great deal of useful cross fertilization between the various schools of thought in addressing the very difficult issues of concurrent systems. Over the years Hoare, Kahn, MacQueen, Milner, Petri, Plotkin, and Pratt, have provided fruitful interaction on the development of the actor model.

Landin [65] first showed how *Algol 60* programs could be represented in applicative-order λ-calculus. Kahn and MacQueen [77] developed this area further by expanding on the construct of *streams* which captured functional systems. Brock and Ackerman [77] extended the Kahn-MacQueen model with the addition of inter-stream ordering information in order to make it more suitable for concurrent computation. Pratt [82] generalized the functional model by developing a theory of processes in terms of sets of partially ordered multisets (*pomsets*) of events. Each pomset in Pratt's *Process Model* represents a *trace* of events. Pratt's model satisfies several properties desirable in any model of concurrent computation. For example, the model does not assume the existence of global states: a trace is only a partial order of events. Thus the model is compatible with the laws of parallel processing formulated in [Hewitt and Baker 77] and shown to be consistent in [Clinger 81].

On the practical side, McCarthy [59] first made functional programming available by developing LISP. The standard dialect of LISP now incorporates lexical scoping and closures which makes the semantics simpler and programming modular [Steele, *et al* 84]. *Act3* generalizes the lexical scoping and upward closures of LISP in the context of parallel systems.

Hoare [78] proposed a language for concurrency, called *CSP*, based on sequential processes. *CSP*, like *Act3*, enhances modularity by not permitting any shared variable between processes; instead, communication is the primitive by which processes may affect each other. At a more theoretical level, Milner [80] has proposed the *Calculus of Concurrent Systems (CCS)*.

One of the nice properties of *CCS* is its elegant algebraic operations. In both *CSP* and *CCS*, communication is synchronous and resembles a handshake. In contradistinction, the actor model postulates the existence of a mail system which buffers communication.

The plan of this paper is as follows: the first section outlines the actor model. The second section describes the *Act3* language. The final section discusses the general principles of open systems and there relation to the actor model.

2 The Actor Model

In this section we motivate the primitives of the actor model. We will outline the basic issues and describe a set of minimal constructs necessary for an actor language.

2.1 Foundational Issues

A number of difficult open problems and foundational issues in the design of programming languages for concurrent systems merit attention. We consider the following three significant:

1. **Shared Resources.** The programming model must deal with the problem of shared resources which may change their internal state. A simple example of such an object in a concurrent environment is a shared bank account. Purely functional systems, unlike object-based systems, are incapable of implementing such objects [Hewitt, *et al* 84].

2. **Dynamic Reconfigurability.** The programming model must deal with the creation of new objects in the evolution of the system. In particular, to accommodate the creation of new objects, there must be a mechanism for communicating the existence of such new objects (or processes) to already existing ones. Thus when a bank creates a new account, it should be able to inform its book-keeping process of the existence of such an account. Since the interconnection topology of processes is static in systems such as *CSP* and *dataflow* [Brock 83], this requirement is necessarily violated these systems.

3. **Inherent Parallelism.** The programming model should exhibit inherent parallelism in the sense that the amount of available concur-

rency should be clear from the structure of programs. It should not be necessary to do extensive reasoning to uncover implicit parallelism that is hidden by inappropriate language constructs. In particular, the assignment command is a bottleneck inherited from the von Neumann architecture. Assignment commands tie the statements in the body of a code in such a way that only through flow analysis is it possible to determine which statements can be executed concurrently. Functional Programming has the advantage of being inherently parallel because it allows the possibility of concurrent execution of all subexpressions in a program [Backus 78].

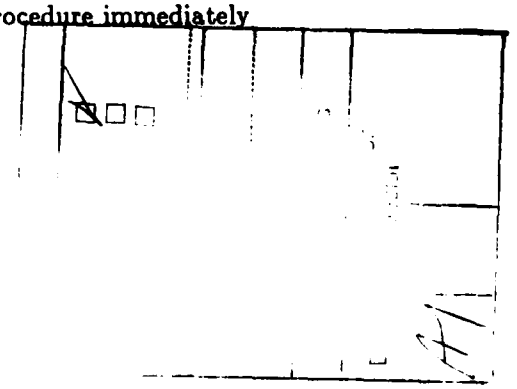
The object-based and functional, λ-calculus-based languages represent two of the most important schools of thought in programming language theory today. As the above discussion suggests, both have certain advantages. *Act3* attempts to integrate both in a manner that preserves some of their attractive features.

2.2 Basic Constructs

The actor abstraction has been developed to exploit message-passing as a basis for concurrent computation [Hewitt 77; Hewitt and Baker 77]. The actor construct has been formalized by providing a mathematical definition for the behavior of an actor system [Agha 85]. Essentially, an actor is a computational agent which carries out its actions in response to processing a communication. The actions it may perform are:

- Send communications to itself or to other actors.
- Create more actors.
- Specify the *replacement behavior*.

In order to send a communication, the sender must specify a mail address, called the *target*. The *mail system* buffers the communication until it can be delivered to the target. However, the order in which the communications are delivered is nondeterministic. The buffering of communications has the consequence that actor languages support recursion. In languages relying on synchronous communication, any recursive procedure immediately leads to *deadlock* [Hewitt, *et al* 1984] [Agha 1985].



All actors have their own (unique) mail addresses which may be communicated to other actors just as any other value. Thus mail addresses provide a simple mechanism for *dynamically reconfiguring* a system of actors. The only way to affect the behavior of an actor is to send it a communication. When an actor accepts a communication, it carries out the actions specified by its behavior; one of these actions is to specify a *replacement actor* which will then accept the next communication received at the mail address.

Two important observations need to be made about replacement. First, replacement implements local state change while preserving *referential transparency* of the identifiers used in a program. An identifier for an object always denotes that object although the behavior associated with the object may be subject to change. In particular, the code for an actor does not contain spurious variables to which different values are assigned (see [Stoy 77] for a thorough discussion of referential transparency). Second, since the computation of a replacement actor is an action which may be carried out concurrently with other actions performed by an actor, the replacement process is intrinsically concurrent. The replacement actor cannot affect the behavior of the replaced actor.

The net result of these properties of replacement actors is that computation in actor systems can be speeded-up by *pipelining* the actions to be performed. As soon as the replacement actor has been computed, the next communication can be processed even as other actions implied by the current communication are still being carried out. In actor-based architectures, the only constraints on the speed of execution stem from the logical dependencies in the computation and the limitations imposed by the hardware resources. In von Neumann architectures, the data dependencies caused by assignments to a global store restrict the degree of pipelining (in the form of instruction pre-fetching) that can be realized [Hwang and Briggs 84].

All actors in a system carry out their actions concurrently. In particular, this has the implication that message-passing can be used to spawn concurrency: An actor, in response to a communication, may send several communications to other actors. The creation of new actors also increases the amount of parallelism feasible in a system. Specifically, *continuations* can be incorporated as first-class objects. The dynamic creation of *customers* in actor systems (discussed later) provides a parallel analogue to such continuations.

2.3 Transitions on Configurations

To describe an actor system, we need to specify several components. In particular, we must specify the behaviors associated with the mail addresses internal to the system. This is done by specifying a *local states function* which basically gives us the behavior of each mail address (i.e., its response to the next communication it receives). We must also specify the unprocessed communications together with their targets. The communication and target pairs are referred to as *tasks*. A *configuration* is an instantaneous snapshot of an actor system from some viewpoint. Each configuration has the following parts:

- A *local states function* which basically gives us the behavior of a mail address. The actors whose behaviors are specified by the local states function are elements of the *population*.
- A set of *unprocessed tasks* for communications which have been sent but not yet accepted.
- A subset of the population, called *receptionist* actors, which may receive communications from actors outside the configuration. The set of receptionists can not be mechanically determined from the local states function of a configuration: it must be specified using knowledge about the larger environment.
- A set of *external actors* whose behavior is not specified by the local states function, but to whom communications may be sent.

A fundamental transition relation on configurations can be defined by applying the behavior function of the target of some unprocessed task to the communication contained in that task (see the definition below). Given the nondeterminism in the *arrival order* of communications, this transition relation represents the different possible paths a computation may take. The processing of communications may, of course, overlap in time. We represent only the acceptance of a communication as an event. Different transition paths may be observed by different viewpoints, provided that these paths are consistent with each other (i.e. do not violate constraints such as causality).

Definition 1 Possible Transition. *Let c_1 and c_2 be two configurations. c_1 is said to have a possible transition to c_2 by processing a task τ, symbolically, $c_1 \xrightarrow{\tau} c_2$ if $\tau \in tasks(c_1)$, and furthermore, if α is the target of the*

of the task then the tasks in c_2 are

$$tasks(c_2) = (tasks(c_1) - \{\tau\}) \cup T$$

where T is the set of tasks created by α in response to τ, and the actors in c_2 are

$$actors(c_2) = (actors(c_1) - \{\alpha\}) \cup A \cup \{\alpha'\}$$

where A are the actors created by α in response to τ and α' is the replacement specified by α. Note that α and α' have the same mail address.

In the actor model, the delivery of all communications is guaranteed. This form of fairness can be expressed by defining a second transition relation which is based on processing finite sets of tasks until a particular task is processed, instead of simply processing a single task [Agha 84]. A denotational semantics for actors can be defined in terms of the transition relations; this semantics maps actor programs into the initial configuration they define [Agha 85].

3 The Act3 Language

Act3 is an actor-based programming language which has been implemented on the *Apiary architecture*. The Apiary is a parallel architecture based on a network of Lisp machines and supports features such as dynamic load balancing, real-time garbage collection, and the mail system abstraction [Hewitt 80]. *Act3* is a descendant of *Act2* [Theriault 83] and is written in a LISP-based interface language called *Scripter*.

A program in *Act3* is a collection of behavior definitions and commands to create actors and send communications to them. A behavior definition consists of an identifier (by which the actor may be known), a list of the names of acquaintances, and a script (which defines the behavior of the actor in response to the communication it accepts). When an actor is created its acquaintances must be specified. For example, a `bank-account` actor may have an acquaintance representing its current balance.

When a communication is accepted by an actor, an environment is defined in which the script of the actor is to be executed. The commands in the script of an actor can be executed in parallel. Thus *Act3* differs fundamentally from programming languages based on communicating sequential processes since the commands in the body of such processes must be executed sequentially.

We will first provide the syntax for a kernel language, *Act*, and use it to explain the basic concepts of message-passing. We then discuss some extensions to *Act* which are provided in *Act3*. Finally, we illustrate these extensions by means of examples.

3.1 The Kernel Language Act

The language *Act* is a sufficient kernel for the *Act3* language: all constructs in the *Act3* language can be translated into *Act* [Agha 85]. Since there are so few constructs in *Act*, it will be easier to understand the primitives involved by studying *Act*. The acquaintance list in *Act* is specified by using identifiers which match a pattern. The pattern provides for freedom from *positional* correspondence when new actors are created. Patterns are used in pattern matching to bind identifiers, and authenticate and extract information from data structures. The simplest pattern is a *bind pattern* which literally binds the value of an identifier to the value of an expression in the current environment. We will not concern ourselves with other patterns here.

When an actor accepts a communication it is *pattern-matched* with the *communication handlers* in the actor's code and dispatched to the handler of the pattern it satisfies. The bindings for the communication list are extracted by the pattern matching as well. The syntax of behavior definitions in *Act* programs is given below.

```
⟨act program⟩ ::=
   ⟨behavior definition⟩* (⟨command⟩*)
⟨behavior definition⟩ ::=
   (define (id {(with identifier ⟨pattern⟩) }*)
               ⟨communication handler⟩*)
⟨communication handler⟩ ::=
   (Is-Communication ⟨pattern⟩ do ⟨command⟩*)
```

The syntax of commands to create actors and send communications is the same in actor definitions as their syntax at the program level. There are four kinds of commands; we describe these in turn. *send commands* are used to send communications. The syntax of the *send command* is the keyword send followed by two expressions: The two expressions are evaluated; the

first expression must evaluate to a mail address while the second may have an arbitrary value. The result of the send command is to send the value of the second expression to the target specified by the first expression. *let commands* bind expressions to identifiers in the body of commands nested within their scope. In particular, *let commands* are used to bind the mail addresses of newly created actors. *new expressions* create new actors and return their mail address. A *new expression* is given by the keyword new followed by an identifier representing a behavior definition, and a list of acquaintances.

The *conditional command* provides a mechanism for branching, and the *become command* specifies the replacement actor. The expression in the *become command* may be a *new expression* in which case the actor becomes a forwarding actor to the actor created by the *new expression*; in this case the two actors are equivalent in a very strong sense. The expression can also be the mail address of an existing actor, in which case all communications sent to the replaced actor are forwarded to the existing actor.

```
⟨command⟩ ::= ⟨let command⟩ | ⟨conditional command⟩ |
              ⟨send command⟩ | ⟨become command⟩

⟨let command⟩ (let (⟨let binding⟩*) do ⟨command⟩*)

⟨conditional command⟩ ::= (if ⟨expression⟩
                              (then do ⟨command⟩*)
                              (else do ⟨command⟩*))

⟨send command⟩ ::= (send ⟨expression⟩ ⟨expression⟩)

⟨become command⟩ ::= (become ⟨expression⟩)
```

A Recursive Factorial. We first provide a simple factorial example to illustrate the use of message-passing in actors to implement control structures. The code makes the low level detail in the execution of an actor language explicit. We will subsequently provide some higher-level constructs which will make the expression of programs easier. The factorial actor creates *customers*, called `FactCust`, whose behavior is also given below. Note that the behavior of a factorial is *unserialized*, i.e, it is not history sensitive.

```
(define (Factorial( ))
  (Is-Communication (a doit (with customer ≡m)
                            (with number ≡n)) do
      (become Factorial)
      (if (NOT (= n 0))
        (then (send m 1))
        (else (let (x = (new FactCust (with customer m)
                                      (with number n)))
                (send Factorial (a do (with customer x)
                                      (with number n-1))))))))

(define (FactCust (with customer ≡m)
                  (with number ≡n))
    (Is-Communication (a number k) do
        (send m n*k)))
```

The acceptance of a communication containing an integer by `Factorial` causes `n` to be bound to the integer and concurrently for factorial to become "itself" so that it can immediately process another integer without any interaction with the processing of the integer it has just received. When the factorial actor processes a communication with a non-zero integer, n, it will:

- Create an actor whose behavior will be to multiply n with an integer it receives and send the reply to the mail address to which the factorial of n was to be sent.
- Send itself the "request" to evaluate the factorial of $n - 1$ and send the value to the customer it created.

The customer created by the factorial actor is also an independent actor. The work done to compute a factorial is conceptually distributed by the creation of the customer. In particular, this implies that computation can be speeded-up if several factorials are to be evaluated concurrently. In the case of the factorial, the same result can be obtained by multiple activations of a given function. However, the solution using multiple activations does not work if the behavior of an actor is serialized.

3.2 Functional Constructs

In this section we will develop some notation for representing expressions at a higher-level. *Act3* provides many such constructs which make *Act3* far more expressive than *Act*, although the two languages have the same

expressive power. To allow functional programming without forcing the programmer to explicitly create the customers, *Act3* provides *call expressions* which automatically create a customer and include its mail address in the communication sent; the value of the *expression* is returned (in a message) to the customer created at the time of the call. The code below specifies a factorial actor in expressional terms. By comparing the code to that in the previous section, one can see how it is executed in an actor-based environment.

```
(define (call Factorial (with number ≡n))
    (if (= n 0)
        (then 1)
        (else (* n (call Factorial (with number n-1))))))
```

Parallel control structures can also be specified quite easily. For example, a parallel algorithm for evaluating the factorial function of n is by recursively subdividing the problem of computing the range product from 1 to n. We define an actor, RangeProduct, for recursively computing the range product in the above manner. The code for Rangeproduct is given below. Note that the One-Of construct provides a generalized conditional command: it dispatches on the value of the expressions (cf. the guarded command [Dijkstra 76]).

```
(define (call RangeProduct (with low ≡lo)
                           (with High ≡hi))
   (One-Of
       (if (= lo hi) lo)
       (if (> lo hi) 1)
       (if (< lo hi)
           (Let ((mid = (/ (+ lo hi) 2)))
              (* (call Rangeproduct (with low lo)
                                    (with high mid))
                 (call Rangeproduct (with low (+ mid 1))
                                    (with high hi)))))))
```

The pipelining of the replacement actors implies that two calls to the RangeProduct actor are in fact equivalent to creating two actors which function concurrently. This equivalence follows from the unserialized nature of the behavior: In case the behavior is unserialized, the behavior of the replacement is known immediately and thus its computation is immediate; in particular, it can be computed even before a communication is received.

Act3 provides a number of other expressional constructs, such as delayed expressions and allows one to require *lazy* or *eager* evaluation strategies for expressions. Such evaluation strategies have been used in extensions of pure functional programming to model *history-sensitive* behavior [Henderson 80]. However, because these systems lack a mail address abstraction, the interconnection network topology of processes is entirely static.

3.3 Modelling Local-State Change

A problem with functional programming is the difficulty of dealing with shared objects which have changing local states. Some constructs, such as *delayed expressions* have been defined to model changing local states. However, the problem with these techniques is that they create expressional forms totally local to the caller and thus can not be used to represent shared objects. Actors permit a graceful implementation of shared objects with a changing local state. The example below shows the implementation of a bank account in *Act3*. A bank account is a canonical example of a shared object with a changing local state.

We use the keyword Is-Request to indicate a request communication is expected. A *request* communication comes with the mail address of the *customer* to which the *reply* is to be sent. The customer is used as the target of the reply. A *request* also specifies a mail address to which a *complaint* can be sent, should the request be unsuccessful. From a software point of view, providing independent targets for the complaint messages is extremely useful because it allows the error-handling to be separated from successfully completed transactions.

```
(define (Account (with Balance ≡b))
   (Is-Request (a Balance) do (reply b))
   (Is-Request (a Deposit (with Amount ≡a)) do
      (become (Account (with Balance (+ b a))))
      (reply (a Deposit-Receipt (with Amount a))))
   (Is-Request (a Withdrawal (with Amount ≡a)) do
      (if (> a b)
       (then do (complain (an Overdraft)))
       (else do
         (become (Account (with Balance (- b a))))
         (reply (a Withdrawal-Receipt (with Amount a)))))))
```

Note that the become command is pipelined so that a replacement is available as soon as the *become command* is executed. The commands for other actions are executed concurrently and do not affect the replacement actor which will be free to accept further communications.

3.4 Transactional Constructs

Analyzing the behavior of a typical program in terms of all the transitions it makes is not very feasible. In particular, the development of *debugging tools* and *resource management* techniques requires us to preserve the abstractions in the source programs. Because actors may represent shared objects, it is often critical that transitions relevant to independent computations be kept separate. For example, if the factorial actor we defined is asked to evaluate the factorial of -1, it will create an "infinite loop." Two observations should be made about such potentially infinite computations. First, any other requests to the factorial will not be affected because the guarantee of delivery means that communications related to those requests will be interleaved with the "infinite loop" generated by the -1 message. Second, in order to keep the performance of the system from degrading, we must assess costs for each "computation" independently; we can then cut-off those computations that we do not want to support indefinitely.

To formalize the notion of a "computation," we define the concept of *transactions*. Transactions are delineated using two specific kinds of communications, namely, *requests* and *replies*. A request, r_1, may trigger another request, say r_2; if the reply to r_2 also precedes the reply to r_1, then the second transaction is said to be *nested* within the first. Proper nesting of transactions allows simpler resource management schemes since resources can be allocated dynamically for the sub-transaction directly from the triggering transaction.

Transactions also permit the development of *debugging* tools that allow one to examine a computation at different levels of granularity [Manning 84]. Various constructs in *Act3* permit proper nesting of transactions; for example, requests may be buffered while simultaneously preserving the current state of a server using a construct called *enqueue*. The request is subsequently processed, when the server is free to do so, using a *dequeue* operation. Enqueue and dequeue are useful for programming servers such as those controlling a hard copy device; they guarantee continuous availability [Hewitt *et al* 1984].

Independent transactions may affect each other; requests may be sent

to the same actor whose behavior is history-sensitive thus creating events which are shared between different transactions. Such intersection of events creates interesting problems for the dynamic allocation of resources and for debugging tools. Dynamic transaction delimitation remains an exciting area of research in the actor paradigm.

4 Open Systems

It is reasonable to expect that large-scale parallel systems will be composed of independently developed and maintained modules. Such systems will be open-ended and continually undergoing change [Hewitt and de Jong 85]. Actor languages are intended to provide linguistic support for such *open systems*. We will briefly outline some characteristics of open systems and describe how the actor model is relevant to the problem of open systems.

4.1 Characteristics of Open Systems

We list three important considerations which are relevant to any architecture supporting large-scale parallelism in open systems [Hewitt 85]. These considerations have model theoretic implications for an algebra used to characterize the behavior of actors:

- *Continuous Availability*. A system may receive communications from the external environment at any point in time. There is no closed-world hypothesis.
- *Modularity*. The inner workings of one subsystem are not available to the any other system; there is an arms-length relationship between subsystems. The behavior of a system must be characterized only in terms of its interaction with the outside.
- *Extensibility*. It is possible for a system to grow. In particular, it is possible to compose different systems in order to define larger systems.

Actors provide an ideal means of realizing open systems. In the section below, we outline a model which realizes the above characteristics and, at the same time, abstracts the internal events in an actor system. We thus address the problem of abstraction in the context of open system modelling.

4.2 A Calculus of Configurations

We have described two transition relations on configurations (see §2.3). These relations are, however, operational rather than extensional in nature. The requirements of modularity imply that an abstract characterization of the behavior of an actor system must be in terms of communications received from outside the system and those sent to the external actors. All communications sent by actors within a population, to other actors also within the population, are not observable from the outside.

In the denotational semantics of sequential programming languages, it is sufficient to represent a program by its input-output behavior, or more completely, as a map from an initial state to a final state (the so-called *history relation*). However, in any program involving concurrency and nondeterminism, the history relation is not a sufficient characterization. Specifically, when two systems with identical history relations are each composed with an identical system, the two resulting systems have different history relations [Brock and Ackerman 81]. The reason for this anomaly is the closed-world assumption inherent in the history relation: It ignores the possible interactions of the output with the input [Agha 85].

Instead, we represent the behavior of a system taking into account the fact that communications may be accepted from the outside at any point. There are three kinds of derivations from a configuration:

1. A configuration c is said to have a derivation to c' given an *input task* τ, symbolically, $c \stackrel{+\tau}{\Longrightarrow} c'$, if

$$\begin{aligned} &\mathit{states}(c') = \mathit{states}(c) \\ &\mathit{tasks}(c') = \mathit{tasks}(c) \cup \tau \ \wedge \ \mathit{target}(\tau) \in \mathit{population}(c) \end{aligned}$$

   where *states* represents the local states function (see §2.3), and *tasks* represents the tasks in a configuration. The receptionists remain the same but the external actors may now include any actors whose mail addresses have been communicated by the communication accepted.

2. A configuration c is said to have a derivation to c' producing an *output task* τ, symbolically, $c \stackrel{-\tau}{\Longrightarrow} c'$, if

$$\begin{aligned} &\mathit{states}(c') = \mathit{states}(c) \\ &\mathit{tasks}(c') = \mathit{tasks}(c) - \tau \ \wedge \ \mathit{target}(\tau) \notin \mathit{population}(c) \end{aligned}$$

   where the *states* and the *tasks* are as above, and "$-$" represents set theoretic difference. The external actors of c' are the same as those of

c. The receptionists may now include all actors whose mail addresses have been communicated to the outside.

3. A configuration c has a *internal* or silent derivation to a configuration c', symbolically, $c \stackrel{\ell}{\Longrightarrow} c'$, if it has a possible transition to c' for some task τ in c.

We can now build a calculus of configurations by defining operations such as composition, relabeling (which changes the mail addresses), restriction (which removes a receptionist), etc. We give the axioms of compositionality to illustrate the calculus of configurations.

Definition 2 Composition. *Let $c_1 \parallel c_2$ represent the (concurrent) composition of c_1 and c_2. Then we have the following rules of derivation about the composition:*

1. *(a) Let τ be a task whose target is in c_1, then*

$$\frac{c_1 \stackrel{+\tau}{\Longrightarrow} c_1' \ , \ c_2 \stackrel{-\tau}{\Longrightarrow} c_2'}{c_1 \parallel c_2 \stackrel{\ell}{\Longrightarrow} c_1' \parallel c_2'}$$

(b) Let λ be any derivation (input, output, or internal), provided that if λ is an input or output derivation then its sender or target, respectively, is not an actor in c_1, then

$$\frac{c_1 \stackrel{\lambda}{\Longrightarrow} c_1'}{c_1 \parallel c_2 \stackrel{\lambda}{\Longrightarrow} c_1' \parallel c_2}$$

2. *The above rules hold,* mutatis mutandis, *for $c_2 \parallel c_1$.*

The only behavior that can be observed in a system is represented by the "labels" on the derivations from its configurations. These represent the communications between a system and its external environment. Following Milner [80] we can define an *observation equivalence* relation on configurations. The definition relies on equality of all possible finite sequences of communications sent to or received from the external environment (ignoring all internal derivations). One way of formalizing observation equivalence is inductively:

Definition 3 Observation Equivalence. *Let c_1 and c_2 be any two tasks, μ be either an input or an output task, ϱ^* represent any arbitrary (finite) number of internal transitions, and $\stackrel{\varrho^*\mu}{\Longrightarrow}$ represent a sequence of internal transitions followed by a μ transition, and furthermore $\approx_k$ be defined inductively as:*

1. $c_1 \approx_0 c_2$
2. $c_1 \approx_{k+1} c_2$ *if*
   (a) $\forall\mu(if\ c_1 \stackrel{\varrho^*\mu}{\Longrightarrow} c_1'\ then\ \exists c_2'(c_2 \stackrel{\varrho^*\mu}{\Longrightarrow} c_2') \wedge c_1' \approx_k c_2')$
   (b) $\forall\mu(if\ c_2 \stackrel{\varrho^*\mu}{\Longrightarrow} c_2'\ then\ \exists c_1'(c_1 \stackrel{\varrho^*\mu}{\Longrightarrow} c_1') \wedge c_1' \approx_k c_2')$

Now c_1 is said to be observationally equivalent to c_2, symbolically, $c_1 \approx c_2$, if $\forall k(c_1 \approx_k c_2)$.

The notion of observation equivalence is weaker than that of the history relation— it creates fewer equivalence classes and thus distinguishes between more configurations. Specifically, it allows for distinguishing between systems that behave differently in response to new tasks, after having sent some communication to an external actor.

We can characterize actor programs by the equivalence classes of initial configurations they define. Properties of actor system can be established in a framework not relying on a closed-world assumption, while at the same time providing an abstract representation of actor systems that does not rely on the internal details of a systems behavior.

5 Conclusions

Actor languages uniformly use message-passing to spawn concurrency and are inherently parallel. The mail system abstraction permits a high-level mechanism for achieving dynamic reconfigurability. The problem of shared resources with changing local state is dealt with by providing an object-oriented environment without the sequential bottle-neck caused by assignment commands. The behavior of an actor is defined in *Act3* by a script which can be abstractly represented as a mathematical function. It is our claim that *Act3* has the major advantages of object-based programming languages together with those of functional and applicative programming languages.

An actor language also provides a suitable basis for large-scale parallelism. Besides the ability to distribute the work required in the course of a computation, actor systems can be composed simply by passing messages between them. The internal workings of an actor system are not available to any other system. A suitable model to support the composition of different systems is obtained by composing the configurations they may be in.

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