

Mind-Boggling Puzzles, Problems, and Curious Questions to Sharpen Your Brain

From the leading expert on test taking and critical-thinking skills

GARY R. GRUBER, PHD

The World's 200 Hardest **BRAAIN TEASERS**

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This book is dedicated to the thousands of people from all walks of life who have asked me to put these questions in a book and explain the answers, putting the quest for the solutions at rest.

INTRODUCTION

For years, numerous people have asked me to write this book after they were intrigued with working on these and similar problems that appeared in the various newspapers and airline magazines I write for. The problems in this book are my best and most interesting selections that will get you to think and increase your creativity. They will also help you develop your intelligence so that you will do better on all standardized tests , including the SAT, ACT, GMAT, LSAT, and GRE. Most importantly, they will give you something to look forward to and enjoy aside from your daily routine.

Many entries include an interesting anecdote about the problem and why it is so baffling, so you will get insight into a new way to think. I have also provided detailed explanations (some of which I have never before divulged) for the more difficult problems. Whatever your daily routine may be, the brain teasers in this book

will challenge you to use your mind in a highly productive and rewarding way.

MY STORY

When I was in fifth grade, I had to take an IQ test. I scored 90, which is below normal and considered "dull." Although I was not told my IQ, I noticed that my teachers were not paying much attention to me and were patronizing me as if I were stupid. Later, as friends of mine were skipping grades, I was routed to the "dull classes," which embarrassed me and made me feel inferior. I felt as if I would never get far in life.

I was in seventh grade when a math teacher at my junior high school in Brooklyn, New York, told my father that he was shocked that I had only a 90 IQ. To my teacher, I seemed much smarter than that. My father was shocked to learn that I had scored a 90 on the IQ test and obtained an IQ test that was currently being administered. He gave me the test.

However, instead of actually taking it (as I had before), I started looking the test over to see what had caused me to get such a low score. This started my fascination with testing and critical thinking. I realized that certain thinking skills were being tested and that a person could actually develop those skills and hone them. I also noticed that there was a generic process to problem solving and thinking. This process was based on extracting something curious from a problem and using that to find the rest of the solution. This process provided

the mechanism to think by "synthesizing" rather than just panic and rush to find an answer. As my school career unfolded, I increased my IQ to 126. I then increased the development of my thinking skills and obtained a 150.

I developed an obsession with seeing how problems can be solved. I eventually got accepted into an elite high school, and I started commenting on teachers' exams by noting on my paper, "This question could be made more interesting by adding so and so," or "This is a poor question; use this instead of that." Most of my teachers did not find this amusing (I even got detention for this behavior), but a few did—the ones who had a real interest in the learning mechanism. I started to become fascinated in how nature works, why things work the way they do, and how problems can be solved. This launched my interest in physics.

But after receiving my PhD, teaching, doing some high-powered research in physics, and even getting invited all over the world to lecture on some of the theories I developed, I realized that there was a much more serious problem to solve. There were all these young people out there who were branded like I was—dull—and were not given an opportunity to show their true talents and perhaps even genius. I felt like I was living in Thomas Gray's poem "Elegy Written in a Country Churchyard" in which he writes, "Many a flower is born to blush unseen and waste its sweet fragrance on the desert air." I realized I had a mission in life. There are all these people out there who could be great scientists, journalists, or other

professionals, people who could develop their talents and become passionate about their life's work and provide us with the breakthroughs we need so much. Therefore, I turned my interest and passion into the quest for how people can solve problems and learn, and how they can enjoy and develop a passion for learning and problem solving. I devoted my life to test taking, test development, critical thinking, and learning. And to my amazement I noticed, after thirty years of research, that most if not all strategies for thinking, learning, and problem solving are based on common sense and not racking your brain.

THE GEOMETRY PROBLEM THAT STUMPED THE NATION

Some time ago, I wrote an article titled "Are You a Genius?" that was published in newspapers all over the country. It was a twelve-question test to determine genius IQ. I received hundreds of letters from readers who could not solve the last and rather simple-looking geometry question. When I was a high school student in New York, it took me three hours to solve this problem. However, forty years later, even after being able to write thirty books on the subject of test preparation and thinking, even I could not solve the problem—and it was driving me crazy! Was I getting stupider as the years passed?

So I decided to reprint the twelve-question test, and if someone got all twelve questions right, they would be called a super genius. I was hoping someone would be able to solve the last question and then tell me how they did it. I didn't get any answers, but I did receive tons

of letters asking how the twelfth problem could be geometrically solved. People at the highest levels in math at major universities, government agencies, you name it, could not solve the problem.

Then I got an urgent call on a Friday from the Washington Post telling me that they were getting hundreds of calls every few hours asking for a solution to the problem. I told them I could not do it. Well, that wasn't good enough for them. They said I'd better have the solution to them in four days, or else! Or else what? They couldn't sue me. For forty years I couldn't solve the problem and now I had to solve it in four days. Didn't I have better things to do over the weekend? Well, I contacted everyone I knew who was literally a genius in math, including top mathematicians in the country. I contacted fellow math students whom I hadn't talked to in thirty years, who went to school with me, and who were super math savvy and may have seen the problem. They were all eager to work on it. However, Sunday rolled around and no one responded with a solution. People from NASA, major math departments all over the country, and even the top mathematicians at Educational Testing Service (the company that develops the majority of entrance, aptitude, and achievement tests such as the SAT) could not solve the problem. In fact, one person was completely peeved, having worked 10 hours straight without a solution!

Then as a very last resort, I was able, by researching and making about twenty calls, to contact my old math professor who had given me the original problem to work on thirty years ago. But when I

called him (he must have been somewhat senile), he told me that I was late for class and I'd better hand in my assignments. He kept repeating it—what a bummer! The last person on earth who could have given me the answer was incoherent! The next day I frantically called the whiz kids I went to school with who were working on the problem and asked for any hints they thought I might use. Each one of them told me to use my own specific math strategies that I have been writing about for years and using in all my test-preparation and thinking books. For example, in geometry when you want to prove that if two sides of a triangle are equal then the base angles are equal, the strategy you use is to draw a line down the triangle. This works because, almost magically, when you draw something extra, you get something for it—namely more information and an approach to the solution. I never thought about that because I thought this problem was too sophisticated! It was Monday night now and I was working feverishly on the problem using my very own strategies. The morning of the deadline came around, and I had just finished solving the problem. I told this to the Washington Post, and they printed a full-page solution—writing me up as "the super genius."

There are actually now six ways to solve the problem, and in this book I'll show the simplest one. See if you can figure it out. Turn to page 182 for the answer!

Given a triangle ABC, side AB = side AC. Draw a line from C to side AB. Call that line CD. Now draw a line from B to side AC. Call that line BE. Let angle EBC = 60 degrees, angle BCD = 70 degrees,

angle ABE = 20 degrees, and angle DCE = 10 degrees. Now draw line DE. Find angle EDC. Do not do this trigonometrically; do it geometrically to get an exact answer.



Dr. Gary R. Gruber

Note: Figures in this book are not drawn to scale.

THE WORLD'S HARDEST BRAIN TEASERS

Here is a collection of my most interesting and mind-improving brain teasers. Many of the answers should give you a strategy for thinking, which will carry over to many other problems and provide you with thinking and problem-solving methods. There is no time limit for these questions (with exceptions as noted). Be aware that there may be more than one way to arrive at an answer to a question.

Just remember, a person who can solve problems efficiently either knows a particular strategy for the type of problem or extracts something from the problem that is curious to him or her and that leads to the next step toward a solution.

1. Two U.S. coins add up to 30 cents. If one of them is not a nickel, what are the two coins?

 Make one word from all the following jumbled letters: orenodw

- 3. In miles per hour, what is the average rate of a car going 20 mph and traveling back the same distance at 60 mph?
 - (a) 30
 - (b) 40
 - (c) 50
 - (d) 60
 - (e) cannot be determined unless the distance is given

- 4. If you don't know the meaning of the word PRECURSORY, which of the following words do you think means the opposite of PRECURSORY?
 - (a) flamboyant
 - (b) succeeding
 - (c) cautious
 - (d) simple
 - (e) not planned

5. An explorer found a silver coin marked 7 BC. He was told it was a forgery. Why?

6. I have only nickels, dimes, and quarters and have at least one of each type of coin. The total number of coins I have is fifteen and the total value of all the coins is \$1.00. How many of each coin do I have?