

$$\mathbf{M} \mathbf{r} \mathbf{o} \quad \square \square_{\square} + \square_{\square} + \square \square_{\square}$$

$$\begin{aligned} \mathbf{v} \mathbf{C} \mathbf{M} \mathbf{v} \mathbf{C} \quad & \square_{\square} - \square_{\square} + \square \square_{\square} \leq \square \\ & \square \square_{\square} + \square \square_{\square} - \square_{\square} \leq \square \\ & - \square_{\square} \leq -\square \\ & \square_{\square} \leq \square \\ & \square_{\square} \square \square_{\square} \square \square_{\square} \geq \square \end{aligned}$$

$$\begin{aligned} \mathbf{M} \mathbf{a} \mathbf{o} \mathbf{a} \mathbf{C} \quad & \mathbf{a} \mathbf{M} \mathbf{a} \mathbf{o} \mathbf{a} \quad \mathbf{r} \quad \mathbf{a} \mathbf{C} \mathbf{o} \mathbf{C} \mathbf{a} \mathbf{M} \mathbf{a} \\ \mathbf{C} \mathbf{o} \mathbf{a} \mathbf{v} \mathbf{o} \mathbf{M} \mathbf{a} \quad & \mathbf{r} \mathbf{v} \mathbf{M} \mathbf{r} \mathbf{v} \mathbf{C} \mathbf{a} \mathbf{a} \quad \mathbf{v} \mathbf{C} \mathbf{M} \mathbf{v} \mathbf{C} \mathbf{a} \end{aligned}$$

Mr r ooooooooooooo + o o o

$$\left| \begin{array}{c} \square \\ \square \end{array} \right| - \left| \begin{array}{c} \square \\ \square \end{array} \right| + \left| \begin{array}{c} \square \\ \square \end{array} \right| \leq \left| \begin{array}{c} \square \\ \square \end{array} \right|$$

$$\begin{bmatrix} 1 \\ 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} - \begin{bmatrix} 0 \\ 1 \end{bmatrix} \begin{bmatrix} 0 \\ 1 \end{bmatrix} \leq \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$\begin{array}{|c|} \hline \\ \hline \end{array} \begin{array}{|c|} \hline \\ \hline \end{array} - \begin{array}{|c|} \hline \\ \hline \end{array} \begin{array}{|c|} \hline \\ \hline \end{array} \leq - \begin{array}{|c|} \hline \\ \hline \end{array}$$

$$\begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \geq \begin{array}{|c|} \hline \text{ } \\ \hline \end{array}$$

$$\mathbf{nr} \quad \mathbf{ro} \quad \begin{array}{|c|} \hline \mathbf{r} \\ \hline \end{array} + \begin{array}{|c|} \hline \mathbf{r} \\ \hline \end{array} - \begin{array}{|c|} \hline \mathbf{r} \\ \hline \end{array} + \begin{array}{|c|} \hline \mathbf{r} \\ \hline \end{array}$$

$$\begin{array}{|c|} \hline \\ \hline \end{array} + \begin{array}{|c|} \hline \\ \hline \end{array} \begin{array}{|c|} \hline \\ \hline \end{array} \geq \begin{array}{|c|} \hline \\ \hline \end{array}$$

$$- \begin{array}{|c|} \hline \\ \hline \end{array} + \begin{array}{|c|} \hline \\ \hline \end{array} \begin{array}{|c|} \hline \\ \hline \end{array} + \begin{array}{|c|} \hline \\ \hline \end{array} \geq \begin{array}{|c|} \hline \\ \hline \end{array}$$

$$\begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} - \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} - \begin{array}{|c|} \hline \text{ } \\ \hline \end{array} \geq \begin{array}{|c|} \hline \text{ } \\ \hline \end{array}$$

$$\begin{array}{ccccccc} \boxed{} & & \boxed{} & \boxed{} & & \boxed{} & \boxed{} \\ | & & | & | & & | & | \\ \boxed{} & & & & & \boxed{} & \boxed{} \end{array} \geq \boxed{}$$

oæ o a oah Ma s M

!"#\$

4 #8; & (

Given a 2-CNF c

Choose a random assignment f to its variables

repeat *many times*

if f is satisfying output f

else

pick an unsatisfied clause at random

flip one of the variables in this clause

output 'unsatisfiable'

; $0 + (< - / (- /$
!

\$

;

$$0 = 0 + P \begin{pmatrix} P_{1,1} & P_{1,2} & P_{1,j} \\ P_{2,1} & P_{2,2} & P_{2,j} \\ P_{i,1} & P_{i,2} & P_{i,j} \end{pmatrix}$$

$$P_{i,j} = \Pr(X_t = a_j \mid X_{t-1} = a_i)$$

,

$$\begin{pmatrix} 1/2 & 1/4 & 1/4 \\ 1/2 & 0 & 1/2 \\ 1/4 & 1/4 & 1/2 \end{pmatrix}$$

& =

$$\sum_j P_{i,j} = 1$$

% & ,

Formula of total probability: If $A_1, \dots, A_k$ are disjoint event such that $A_1 + \dots + A_k = \text{Sample Space}$, then for any even B

$$\Pr(B) = \Pr(A_1) \Pr(B | A_1) + \dots + \Pr(A_k) \Pr(B | A_k)$$

Let $\{a_1, \dots, a_n\}$ be the states of M.C.

By $p_i(t)$ we denote the probability $\Pr(X_t = a_i)$,

$$p(t) = (p_1(t), \dots, p_n(t))$$

Then by the formula of total probability

$$\Pr(X_t = a_j) = \sum_{i=1}^n \Pr(X_{t-1} = a_i) \Pr(X_t = a_j | X_{t-1} = a_i)$$

$$p_j(t) = \sum_{i=1}^n p_i(t-1) P_{i,j}$$

$$p(t) = p(t-1) P$$